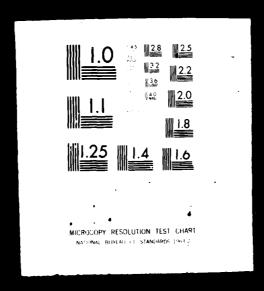
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PRELIMINARY STUDY OF A TEST PROCEDURE FOR OBTAINING STEP WAVE L--ETC(U)

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PRELIMINARY STUDY OF A TEST PROCEDURE FOR OBTAINING STEP **WAVE LOADINGS ON STRUCTURES** AT DEEP SUBMERGENCE

Weidlinger Associates 110 East 59th Street New York, New York 10022

30 April 1979

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A charge designed to produce a step wave would be	placed in the water outside				

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20. ABSTRACT (Continued)

the test device. The shock wave from the charge would thus produce a loading in the pressurized cylinder and hence on the test mode.

One of the first questions that arises is what is the form of the pressure wave that is produced within the cylinder. This report presents a preliminary study of this problem by considering the response of a submerged fluid-filled ring subjected to a transverse step wave. The external fluid is represented by using the plane wave approximation. The ring and internal fluid equations are replaced by finite difference approximations using central differences in space and time. Details of the numerical method, and the results of six calculations are given. In these six calculations, water is used as the internal and external fluids, and the ring, which has the properties of either steel or aluminum, has two different radii and two or three different thicknesses.

The primary reason for these calculations is to determine whether the ring is "transparent." That is, does the internal pressure time history look nearly the same as the external pressure. The results show that the ring is transparent if it is thin enough but, as the thickness increases, strong ring vibrations become important. Nonetheless, it appears that there are realistic ring parameters (moduli, radius, thickness) which make the test procedure feasible. Consequently, it is recommended that a combined experimental-theoretical program be seriously considered.

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INTRODUCTION

This investigation is concerned with the development of a possible technique for obtaining step wave loadings on deeply submerged structures. This type of loading has been successfully obtained at shallow depths, through the use of specially designed charges. For such shallow experiments, the venting of the bubble produced by the explosion has resulted in the alleviation of any bubble pulse effects from the charge, thus resulting in a reasonable pressure wave simulation. For deep submergence applications however, the exploding of a charge produces a bubble where pulsations would produce an additional loading on the model. It is both costly and questionable whether any artificial bubble entrapment mechanisms would work at these depths. Since this additional bubble pulse loading is undesireable for the present purposes, the consideration of some other means of avoiding the bubble became appropriate.

For several years the possibility of utilizing a pressurized cylinder as a test device has been under consideration. The test device cylinder would itself be submerged. Inside the cylinder, a model would be placed and the water brought to the required at-depth pressure for the test. A charge designed to produce a step wave would be placed in the water outside the test device. The shock wave from this charge would thus envelop the test device cylinder, and produce a loading in the pressurized tank and thus on the test model.

One of the first questions that arises is that of the form of the pressure wave that is produced within the test device. We would of course require a plateau-like pressure signal which would be maintained for a minimum of

three transit times of the shock wave across the model. The problem to be investigated thus becomes a question of the transparency of the test device cylinder with respect to the pressure wave from the outside explosion which envelopes it, and thus produces a pressure wave in the internal fluid. Of prime importance is whether or not the wave in the internal fluid can be made to maintain the plateau-like pressure signal for three or more envelopment times of the shock wave across the test model.

This report presents a preliminary study of this problem. It considers the response of a submerged fluid-filled ring subjected to a transverse step wave. The results of particular interest are the pressure signals produced at points in the fluid in the interior of the ring. Details of the numerical methods and the results are given in the following sections.

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NUMERICAL METHOD

A finite difference method is used to study the problem of a submerged fluid-filled ring, subjected to a transverse step wave. The basic equations are written in polar coordinates with sign conventions as shown in Fig. 1.

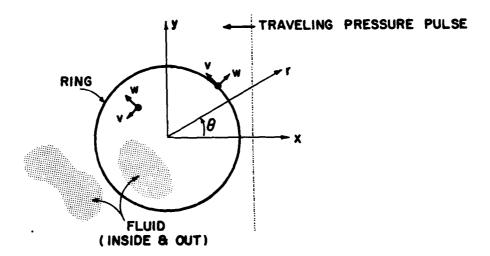


FIG. I FLUID - FILLED RING SUBJECTED TO TRANSVERSE STEP PULSE

The external fluid is represented by using the plane wave approximation. The shell and internal fluid equations are replaced by finite difference approximations using central differences in space and time: thus the time integration method is explicit and numerical stability conditions must be considered. Symmetry in space is taken into account so that only points in $0 \le \theta \le \pi$ are included in the calculation.

Ring Equations

The equations of motion for the ring are based on those in <u>Stresses</u>

in <u>Shells</u> by Wilhelm Flügge (Springer-Verlag, 1960, pp. 208-215), specialized to the case of a ring.

$$\bar{\rho}h \dot{v} = \frac{1}{a} \frac{\partial N}{\partial \theta} - \frac{1}{a^2} \frac{\partial M}{\partial \theta}$$

$$\bar{\rho}h \dot{w} = -\frac{1}{a^2} \frac{\partial^2 M}{\partial \theta^2} - \frac{1}{a} N - (p_{TE} - p_{TI})$$

Here v and w represent the tangential and radial velocities of the shell, M and N the moment and stress resultant, a the shell radius, $\bar{\rho}$ and h the shell density and thickness, and p_{TE} and p_{TI} are the total external and internal pressures. The moment and stress resultant are given by

$$M = K \kappa$$

$$N = D\epsilon + \frac{1}{a} K \kappa$$

with

$$D = \frac{Eh}{(1 - v^2)}$$

and

$$K = \frac{Dh^2}{12}$$

where ν is Poisson's ratio, E is Young's modulus, ϵ is the hoop strain at the center-line, given in incremental form by

$$\dot{\varepsilon} = \frac{1}{a} \left(\frac{\partial \mathbf{v}}{\partial \theta} + \mathbf{w} \right)$$

and K is the curvature, given in incremental form by

$$\dot{\kappa} = \frac{1}{a^2} \left(\frac{\partial^2 w}{\partial \theta^2} + w \right)$$

The finite difference grid for the ring is shown in Fig. 2, with all points equally spaced in the θ -direction (spacing $\Delta\theta$). The quantities w, M, N, ϵ and κ are calculated at θ_i = $i\Delta\theta$ for i = (0, 1,...,n) with the last point θ_n = π . The tangential shell velocity, v, is calculated at midpoints, $\theta_{i+1/2}$ = (i + 1/2) $\Delta\theta$ for i = (0, 1,...,n-1).

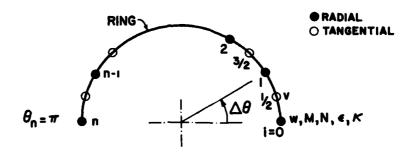


FIG. 2 FINITE DIFFERENCE GRID FOR RING

Let $v_{i+1/2}$ denote $v(\theta_{i+1/2}, t)$. Let w_i denote $w(\theta_i, t)$; similarly for M_i , N_i , ϵ_i , κ_i . The finite difference form of the equations of motion is given by

$$\bar{\rho}h \dot{v}_{i+1/2} = \frac{1}{a\Delta\theta} (N_{i+1} - N_{i}) - \frac{1}{a^{2}\Delta\theta} (M_{i+1} - M_{i})$$

$$\bar{\rho}h \dot{w}_{i} = -\frac{1}{a^{2}\Delta\theta^{2}} (M_{i+1} - 2M_{i} + M_{i-1})$$

$$-\frac{1}{a} N_{i} - (p_{TE} - p_{TI})_{i}$$

The first equation applies for i = (0, 1, ..., n-1); the second applies only for i = (1, 2, ..., n-1). From symmetry, the appropriate form of the second equation, for $\theta_0 = 0$, is given by

$$\vec{p}h \ \dot{w}_0 = -\frac{1}{a^2 \Delta \theta^2} (2M_1 - 2M_0)$$

$$-\frac{1}{a} N_0 - (p_{TE} - p_{TI})_0$$

and for $\theta_n = \pi$,

$$\vec{p}h \stackrel{\cdot}{w}_{n} = -\frac{1}{a^{2}\Delta\theta^{2}} (2M_{n-1} - 2M_{n})$$

$$-\frac{1}{a} N_{n} - (p_{TE} - p_{TI})_{n}$$

The strain rates for i = (1, 2, ..., n-1) are given by

$$\dot{\varepsilon}_{i} = \frac{1}{a\Delta\theta} (v_{i+1/2} - v_{i-1/2}) + \frac{1}{a} w_{i}$$

and the curvature rates by

$$\dot{\kappa}_{i} = \frac{1}{a^{2} \Delta \theta^{2}} (w_{i+1} - 2w_{i} + w_{i-1}) + \frac{1}{a^{2}} w_{i}$$

By symmetry, for $\theta_0 = 0$,

$$\dot{\varepsilon}_{0} = \frac{1}{a\Delta\theta} (2 v_{1/2}) + \frac{1}{a} w_{0}$$

$$\dot{\kappa}_{0} = \frac{1}{a^{2}\Delta\theta^{2}} (2w_{1} - 2w_{0}) + \frac{1}{a^{2}} w_{0}$$

and for
$$\theta_n = \pi$$

$$\dot{\varepsilon}_{n} = \frac{1}{a\Delta\theta} (-2v_{n-1/2}) + \frac{1}{a} w_{n}$$

$$\dot{\kappa}_{n} = \frac{1}{a^{2} \Delta \theta^{2}} (2w_{n-1} - 2w_{n}) + \frac{1}{a^{2}} w_{n}$$

Internal Fluid Equations

The equations of motion in the fluid are those of an inviscid acoustic fluid.

$$\rho \dot{\mathbf{v}} = -\frac{1}{r} \frac{\partial \mathbf{p}}{\partial \theta}$$

$$\rho \dot{\mathbf{w}} = -\frac{\partial \mathbf{p}}{\partial \mathbf{r}}$$

Here v and w are the tangential and radial velocites of the fluid particles, p is the fluid pressure and ρ is the fluid density. The fluid pressure is determined by

$$\dot{p} = -\rho c^2 \frac{1}{r} \left[\frac{\partial (rw)}{\partial r} + \frac{\partial v}{\partial \theta} \right]$$

where c is the fluid wave speed.

The finite difference grid for the fluid (see Fig. 3) is obtained by drawing an even number, 2ℓ , of constant radius lines which are equally spaced in the r-direction. A pressure is associated with the point at r=0. The innermost line and every other line is associated with radial velocities. The remaining lines are associated with pressures and tangential velocities.

The distance $\Delta r = (\frac{2a}{2\ell+1})$ is convenient for writing the finite difference equations. Radial velocity lines are defined at $r_{j+1/2} = (j+1/2) \Delta r$ for $j = (0, 1, \dots, \ell)$, pressure lines at $r_{j} = j\Delta r$ for $j = (0, 1, \dots, \ell)$ and tangential velocity lines at $r_{j} = j\Delta r$ for $j = (1, 2, \dots, \ell)$. Each line (j or j+1/2) is divided into a set of equally spaced points in the θ -direction. Radial velocities and pressures are defined at $\theta=0$ and $\theta=\pi$; tangential velocities are defined at midpoints between the pressure points. The number of pressure points on each line is calculated to maintain arc separation roughly equal to radial separation; that is, $r_{j}\Delta\theta_{j} \cong \Delta r$.

Hence, the number of pressure points on a j-line is variable and chosen to be 3j+1 for $j=(0,1,\ldots,\ell)$. The same number of points is chosen for the next inner (radial velocity) line.

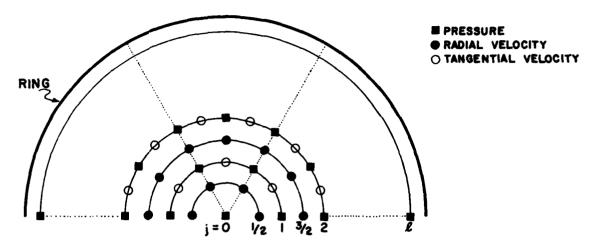


FIG.3 FINITE DIFFERENCE GRID FOR INTERNAL FLUID

Let $p_{j,i}$ denote $p(r_j, \theta_i, t)$, let $v_{j,i+1/2}$ denote $v(r_j, \theta_{i+1/2}, t)$ and let $w_{j+1/2,i}$ denote $w(r_{j+1/2}, \theta_i, t)$. The finite difference equations for the fluid are given by

$$\rho \dot{v}_{j,i+1/2} = -\frac{1}{r_{j}\Delta\theta_{j}} (p_{j,i+1} - p_{j,i})$$

$$\rho \dot{w}_{j+1/2,i} = -\frac{1}{\Delta r} (\bar{p}_{j+1,i} - \bar{p}_{j,i})$$

$$\dot{p}_{j,i} = -\rho c^{2} \left[\frac{(r_{j+1/2} \bar{w}_{j+1/2,i} - r_{j-1/2} \bar{w}_{j-1/2,i})}{r_{j}\Delta r} + \frac{(v_{j,i+1/2} - v_{j,i-1/2})}{r_{j}\Delta\theta_{j}} \right]$$

The over-bar symbol () in the second and third equations indicates that linear interpolation in θ is used since radial velocities and pressures are not always defined at the same θ values.

Special forms of the third equation are needed for r=0, θ =0 and θ = π . For r=0, the average value of the divergence $<\nabla.w>_0$ is used

$$\langle \nabla.w \rangle_0 = \frac{w_{1/2,0} + 2w_{1/2,1} + 2w_{1/2,2} + w_{1/2,3}}{3\Delta r}$$

so that $\dot{p}_{o,o} = -\rho c^2 < \nabla.w >_0$. By symmetry, for $\theta=0$

$$\dot{p}_{j,0} = -\rho c^{2} \left[\frac{(r_{j+1/2} \bar{w}_{j+1/2,0} - r_{j-1/2} \bar{w}_{j-1/2,0})}{r_{j} \Delta r} + \frac{2v_{j,1/2}}{r_{j} \Delta \theta_{j}} \right]$$

and for $\theta=\pi$

$$\dot{p}_{j,3j} = -\rho c^{2} \left[\frac{(r_{j+1/2} \bar{w}_{j+1/2,3j} - r_{j-1/2} \bar{w}_{j-1/2,3j})}{r_{j} \Delta r} - \frac{2v_{j,3j-1/2}}{r_{j} \Delta \theta_{j}} \right]$$

Fluid-Shell Coupling

The internal fluid pressure $p_{TI}^{}$ is determined by using the pressures on the j=l line nearest the ring. Since the θ spacing for the ring is not necessarily the same as that for the j=l pressures, linear interpolation in θ is used to calculate $p_{TI}^{}$.

The effect of the external fluid is represented by the plane wave approximation which, for the transverse step wave traveling in the negative x-direction, is given by

$$P_{TE} = P_0(1 + \cos\theta) H(t + (x-a)/c) + \rho cw$$

Here \mathbf{p}_{TE} is the total exterior pressure in the fluid, \mathbf{P}_0 is the pressure jump, $\mathbf{H}(t)$ is the unit step function, ρ and \mathbf{c} are the fluid density and wave speed and \mathbf{w} is the radial velocity of the shell. In the numerical calculations, the unit step function is replaced by a waveform with a finite rise-time. This modification reduces the high frequency components in the computed results.

Time Integration

The time integration method for the ring and internal fluid is explicit (based on central differences) and uses a constant time step, Δt , which is determined by numerical stability considerations. Appropriate initial values of velocities and stress-type quantities (M, N and p) are assumed to be known and the following iterative procedure is used. Accelerations (radial and tangential) are calculated from spatial differences of stress-type quantities. Let Δ_k denote such an acceleration at time $t_k = k\Delta t$. Velocities at time $t_{k+1/2} = (k+1/2)\Delta t$, denoted by $V_{k+1/2}$, are calculated by

$$V_{k+1/2} = V_{k-1/2} + \Delta t A_k$$

Strain rates (or curvature rates, or fluid divergence rates) at time $t_{k+1/2}$, denoted by $E_{k+1/2}$, are calculated from spatial differences of the new velocities. Stress-type quantities at time t_{k+1} , denoted by S_{k+1} , are calculated by

$$S_{k+1} = S_k + \Delta t D \dot{E}_{k+1/2}$$

where D symbolizes the appropriate constitutive relation (pressure-volume, moment-curvature, etc.). These two calculations are performed for all points in the fluid and on the ring.

This method does not use a pseudo-viscosity which is often used in finite difference calculations to remove spurious, high-frequency numerical oscillations. Consequently, high frequency components in the external pressure waveform have been reduced by using a finite rise-time of $10~\text{a/c}(2^{\circ}+1)$ in the unit step function. That is, $10~\Delta t_3$ is used where Δt_3 is defined in the next section.

Numerical Stability

The shell equations are hyperbolic with respect to the tangential displacement and the wave speed of this motion is controlled by $\bar{c}=\sqrt{E/\bar{\nu}(1-\nu^2)}$. The effective separation is $a\Delta\theta$. Hence the numerical stability condition for this effect is taken as

$$\Delta t_1 \leq \frac{a\Delta\theta}{\bar{c}}$$

(The shell equations are parabolic with respect to the radial displacement but for $h \le 2a\Delta\theta$, approximately, the condition from the tangential motion is more critical.) The plane wave approximation contains a viscous damping term which can affect numerical stability for certain ranges of parameters. The condition corresponding to this effect is represented by

$$\Delta t_2 \leq \frac{\overline{\rho}h}{\rho c}$$

The fluid behavior is hyperbolic in both the radial and tangential directions. Numerical stability for this effect is represented by

$$\Delta t_3 \leq \frac{\Delta \ell}{c}$$

where $\Delta \ell$ is the minimum distance between points in the fluid. This corresponds to the distance between the radial velocities which surround the origin (r=0), and thus $\Delta \ell$ = a/(2 ℓ +1)

The time step used in the calculation is determined by

$$\Delta t = s \min(\Delta t_1, \Delta t_2, \Delta t_3)$$

where s = 1/2 has been used as a safety factor.

DISCUSSION OF RESULTS

The results of six calculations are contained in Appendices A, B, C, D, E and F. These calculations correspond to the following six different cases for the ring.

Ring	Material	a=radius (inches)	h=thickness (inches)
A	Steel	200	2
B C	Steel "	100	2 0.5
D E F	Aluminum	100	3.5 1 0.3

All lengths are in inches, pressures are in ksi (kilo-pounds per square inch), and time in milliseconds. Properties of the fluid (inside and out) and the ring are taken as shown in the following tables.

Fluid	$\rho = \text{density } (\text{ksi-msec}^2/\text{in}^4)$	c = wave speed (in/msec)
Water	0.093	59

Material	٩/٩	E = Young's Modulus (ksi)	ν = Poisson's Ratio
Steel	7.8	28,000	0.28
Aluminum	2.7	19,000	0.33

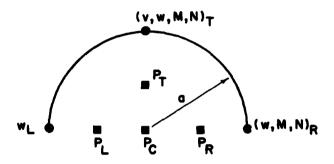
Time t=0 corresponds to first arrival of the external pressure wave at the right side (θ =0) of the ring the external fluid pressure jump is P_0 = 1 ksi. The time scale in case A is 16 msec long but is only 8 msec long in the other five cases (due to change in radius a).

Twelve time histories are shown in each appendix as indicated in Fig. 4.

Curve Label:	Meaning
P-CENTER:	pressure at r = 0
P-RIGHT:	pressure at $r = a/2$, $\theta = 0$
P-TOP:	pressure at $r = a/2$, $\theta = 90$ deg.
P-LEFT:	pressure at $r = a/2$, $\theta = 180$ deg.
SRV-RIGHT:	shell radial velocity at $\theta = 0$
SM-RIGHT:	shell moment at $\theta = 0$
SN-RIGHT:	shell stress resultant at $\theta = 0$
SRV-TOP:	shell radial velocity at θ = 90 deg.
STV-TOP:	shell tangential velocity at $\theta = 90$
SM-TOP:	shell moment at $\theta = 90$

SN-TOP:

SRV-LEFT:



shell stress resultant at θ = 90

shell radial velocity at θ = 180 deg.

FIG. 4 KEY TO TIME HISTORIES IN APPENDICES

All calculations were performed with 31 points on the ring and 651 points in the fluid (ℓ =20) with 61 pressure points adjacent to the ring. A typical calculation of about 500 time steps required about 60 seconds of computer time on the CDC 6600.

Numerical Oscillations

As noted previously, the finite difference equations do not contain any pseudo-viscosity terms. Consequently, the calculated time histories may contain spurious high-frequency numerical oscillations. Most of these oscillations can be removed by making sure that the applied pressure time history is smooth compared to the cut-off frequency of the numerical scheme. This has been done by introducing a finite rise-time of 10 Δt_3 into the external pressure, as noted on pages 10 and 11. However, some time histories show a "beat" phenomenon which appears first in SM-RIGHT (e.g. see case C, t = 3 msec). This beat phenomenon may be the result of numerical oscillations interacting with physical oscillations of ring-fluid system or it may be symptomatic of a real physical effect. Since the plane wave approximation (PWA) is generally good only for early times (ct \tilde{c} 2a), this later time phenomenon may not be important. On the other hand, the PWA is reasonable in this problem, at long times (though possibly not at intermediate times) since the fluid-filled ring is near neutral buoyancy. Further study will be required to understand the beat phenomenon.

Transparency of the Ring

The primary reason for these calculations is to determine whether (or to what extent) the ring is "transparent". That is, does the internal pressure time history look nearly the same as the external pressure – at least for about 3.5 msec. For a sufficiently thin ring this is clearly the case. For example in case F (h/a = 0.003) the pressure at all four interior points is nearly constant and equal to $P_0 = 1$ (within about 10 per cent). In case E (h/a = 0.01) the deviation is more noticeable and in case D (h/a = 0.035) the deviation at the center is about 40 per cent after about 2.5 msec. P-LEFT in case D shows that a small tension wave is

the first signal felt at that point: this is caused by the early radial motion of the ring at θ = 180 deg (see SRV-LEFT). In case D, ring vibrations (primarily the ovaling mode) are so large that the pressure signal at center is significantly altered. The best response in case D is at P-RIGHT (r = a/2, θ =0) where the initial pressure is near p = 1 at about t = 1 and drops to about p = .8 at about t = 3.5 msec. After that time, the strong ring vibrations are apparent and the pressure drops quickly to p = .4.

Comparing the 2 in. thick steel (Case B) with the 3.5 in. thick aluminum (both of radius 100 in.), the aluminum is slightly more transparent than the steel, as expected.

Finally, the larger radius (200 in.) 2 in. thick steel ring shows that, although P-LEFT has a significant deviation from P_0 = 1, P-CENTER drops about 35 per cent after 3.5 msec, and P-RIGHT drops less than 20 per cent after 3.5 msec. In fact, the results in case A (steel, a=200, h=2) look surprisingly like those in case D (alum., a=100, h=3.5) except for the longer time scales in case A (and the related differences in SM-RIGHT, SM-TOP and SN-TOP) caused by the larger radius.

SUMMARY AND CONCLUSIONS

This preliminary study has thus far indicated that pressure signals of acceptable form and duration would probably be produced in the suggested device. It appears to us that additional numerical studies and possible small-scale experimentation should be initiated.

Insofar as the numerical studies are concerned, we would consider the following possibilities:

- (1) Study the beat phenomenon to identify its source and to determine whether it is in fact real.
- (2) Consider a modal type re-calculation. This may make it considerably easier to study the beat phenomena.
- (3) Consider other materials for the test vehicle, eg. rubber or plastics.
- (4) Initiate, in coordination with UERD, a study on charge shaping. The object of this work would be to attempt to produce a pressure signal in the outside fluid which would result in a more plateau-like pressure signal in the interior fluid. Calculations would be made with the prepared new loadings to study this phenomena.

At the same time that the numerical studies are in progress, we strongly recommend that UERD initiate an experimental study of this problem. Experimental verification of the calculated transparency of the shell is required. This can be done to the UERD test basin, using relatively small scale models of different materials and dimensions.

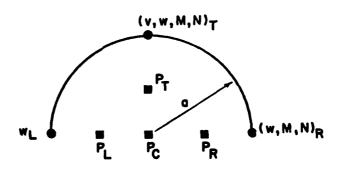
To summarize, preliminary calculations indicate that the idea is feasible and should be seriously studied. The possibility of using existing structures for the test chamber, eg. the AB-1 model, appears attractive and should also be pursued. We also recommend that the additional numerical studies be implemented and that a meeting to discuss the implications of the proposed test device be scheduled at an appropriate time.

APPENDIX A (Case A)

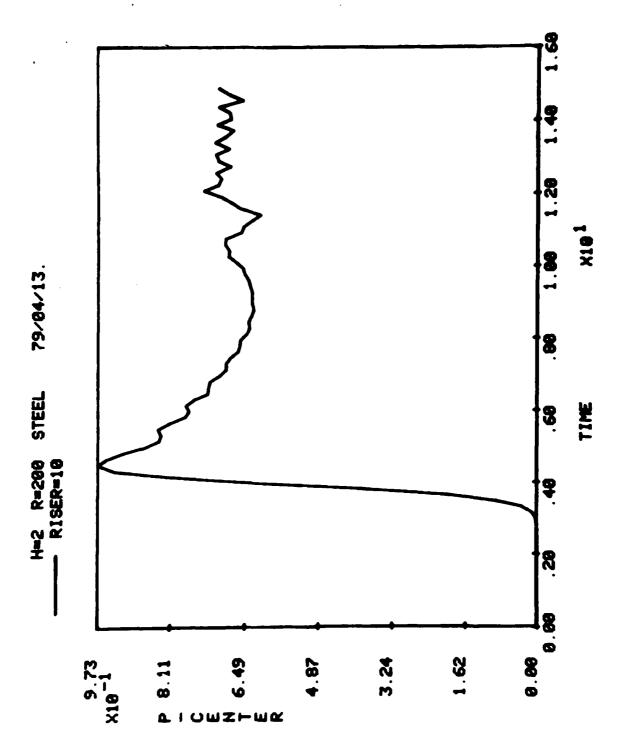
RING: Steel

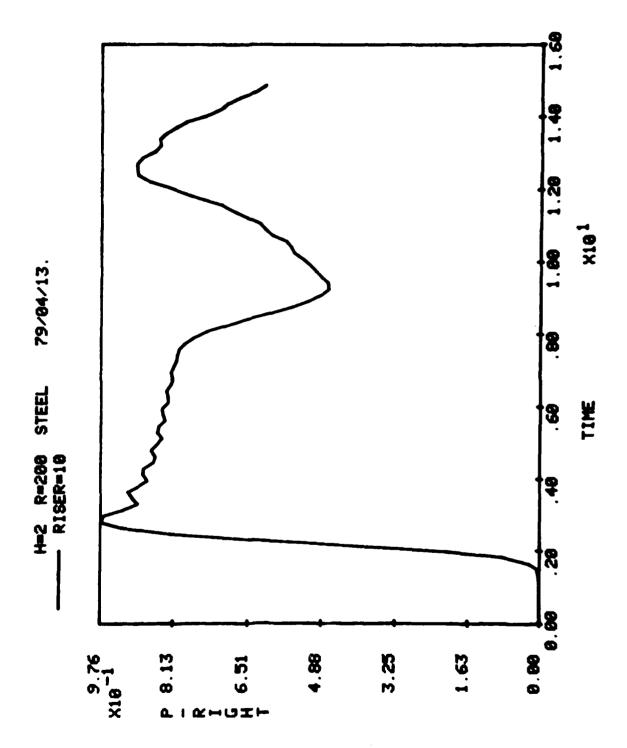
Radius = 200 inches Thickness = 2 inches

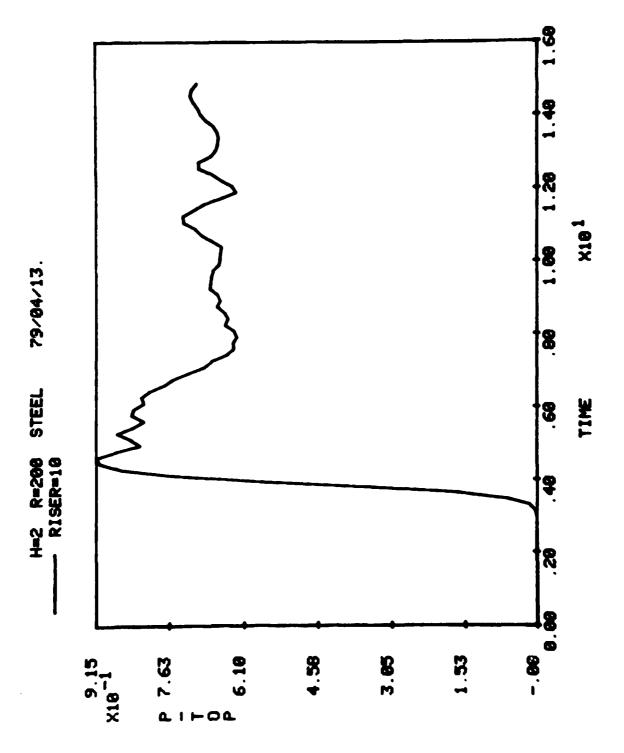
Meaning
pressure at r = 0
pressure at $r = a/2$, $\theta = 0$
pressure at r = $a/2$, θ = 90 deg.
pressure at $r = a/2$, $\theta = 180$ deg.
shell radial velocity at θ = 0
shell moment at $\theta = 0$
shell stress resultant at $\theta = 0$
shell radial velocity at θ = 90 deg.
shell tangential velocity at $\theta = 90$
shell moment at $\theta = 90$
shell stress resultant at $\theta = 90$
shell radial velocity at θ = 180 deg.



KEY TO TIME HISTORIES IN APPENDICES

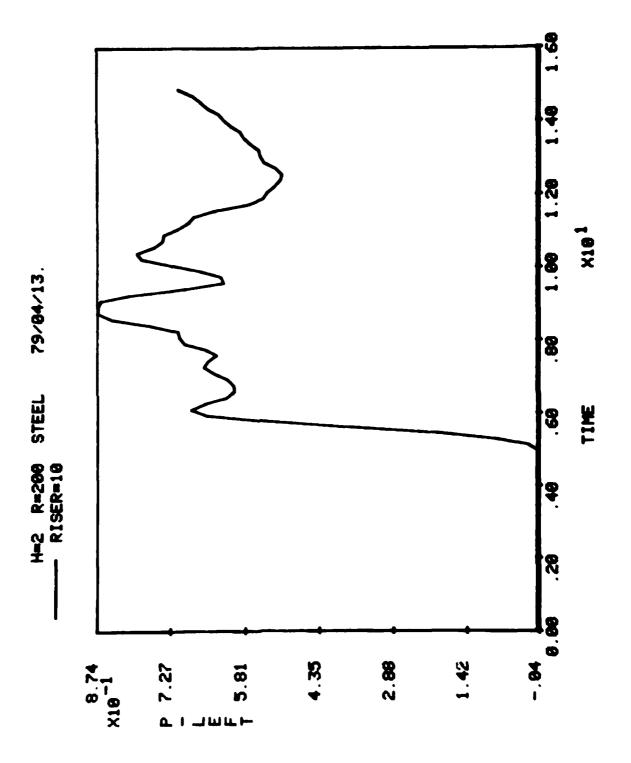






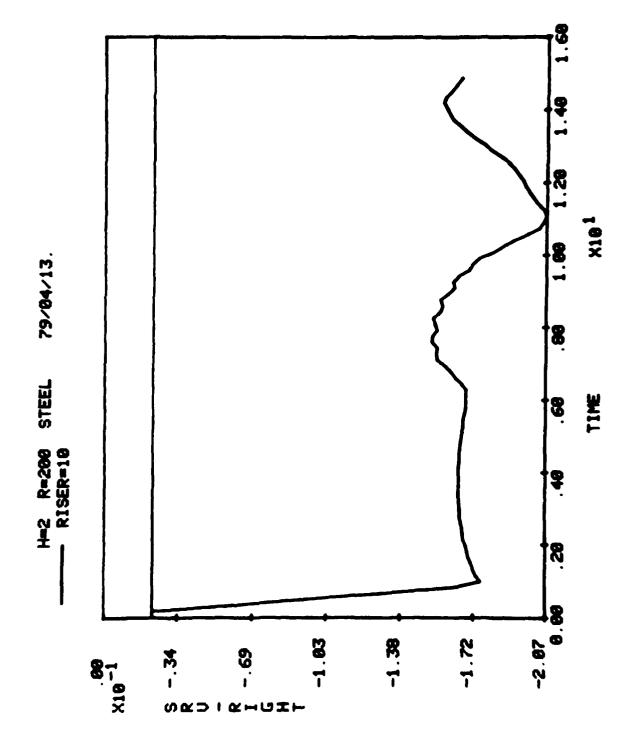
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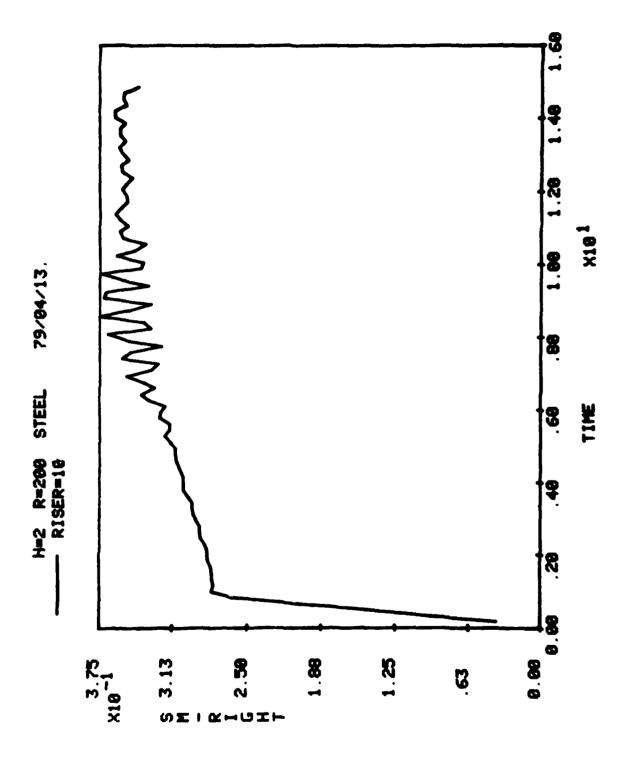
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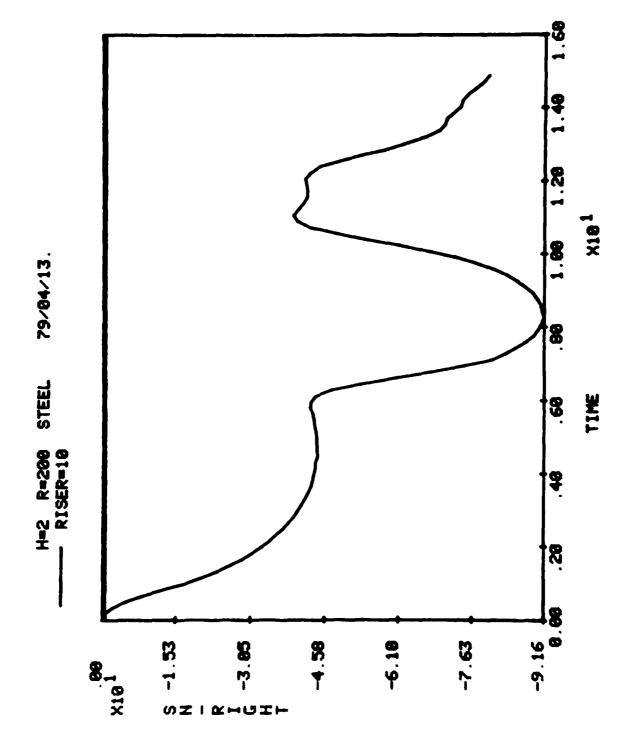
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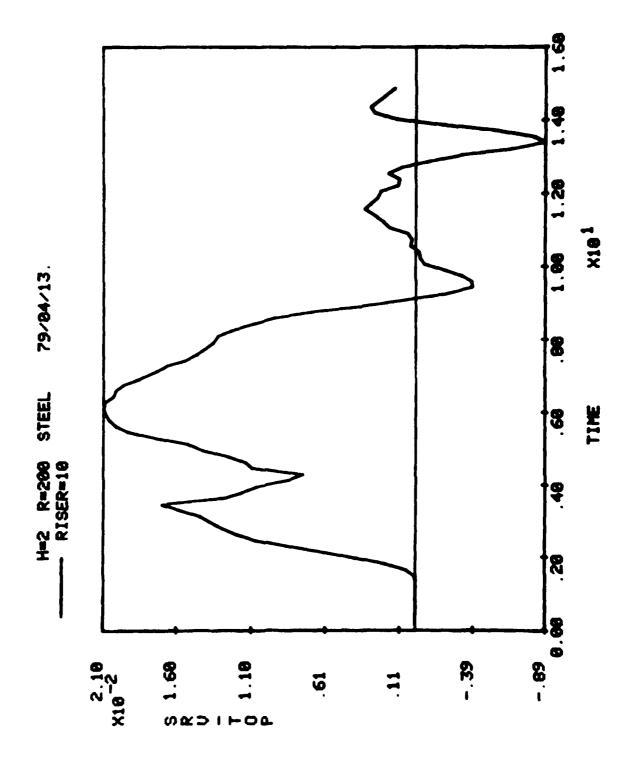
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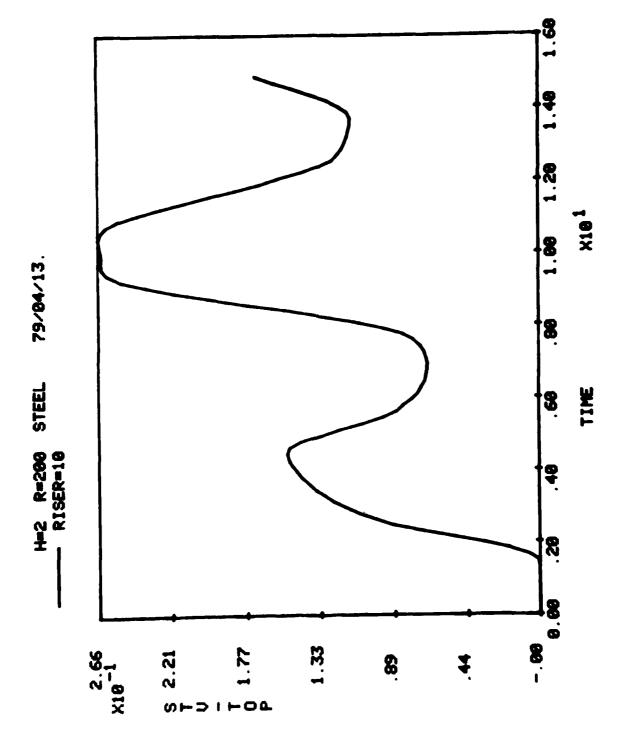


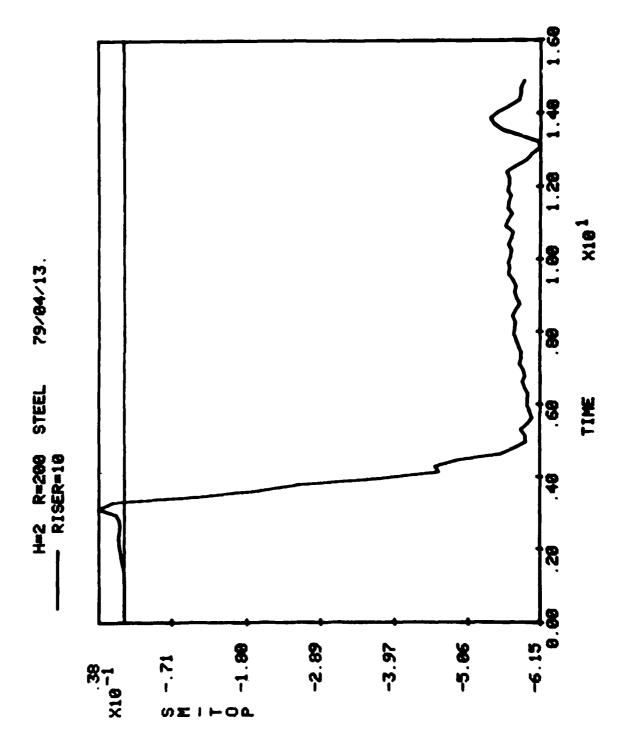


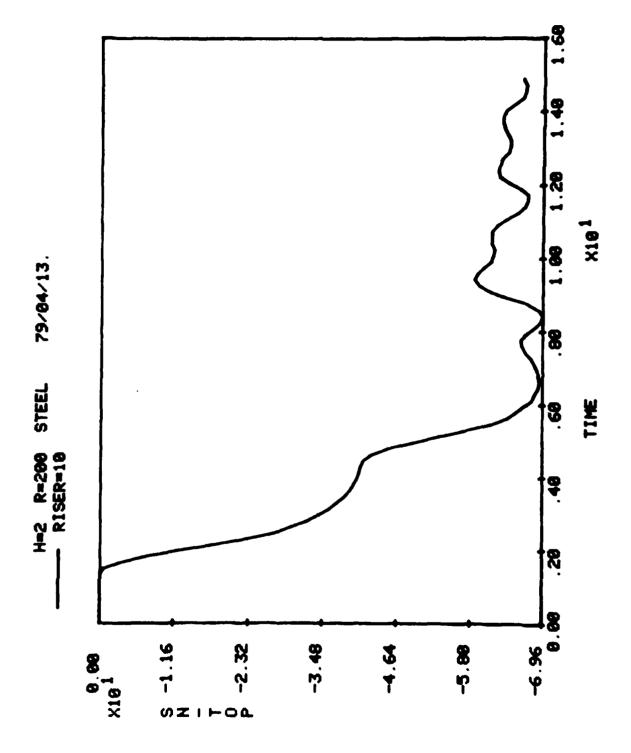
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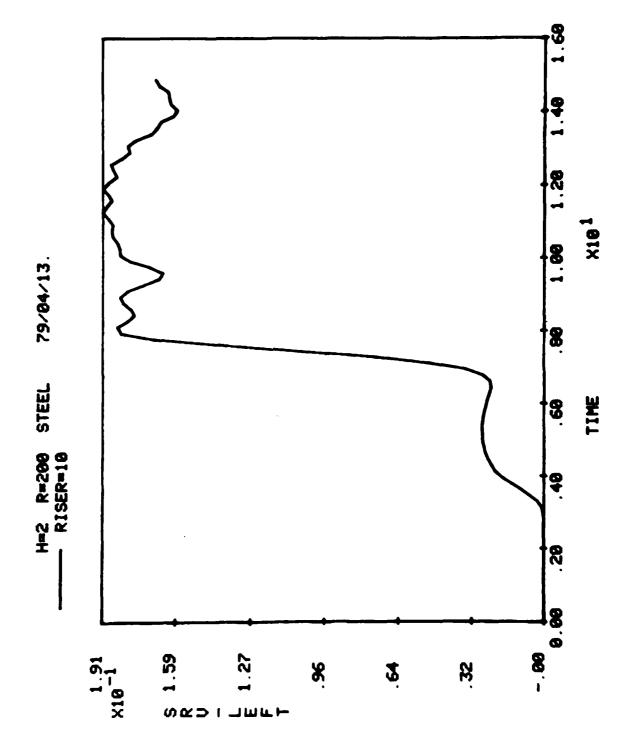












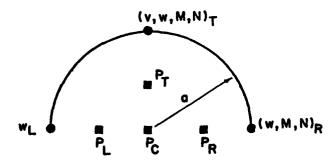
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APPENDIX B (Case B)

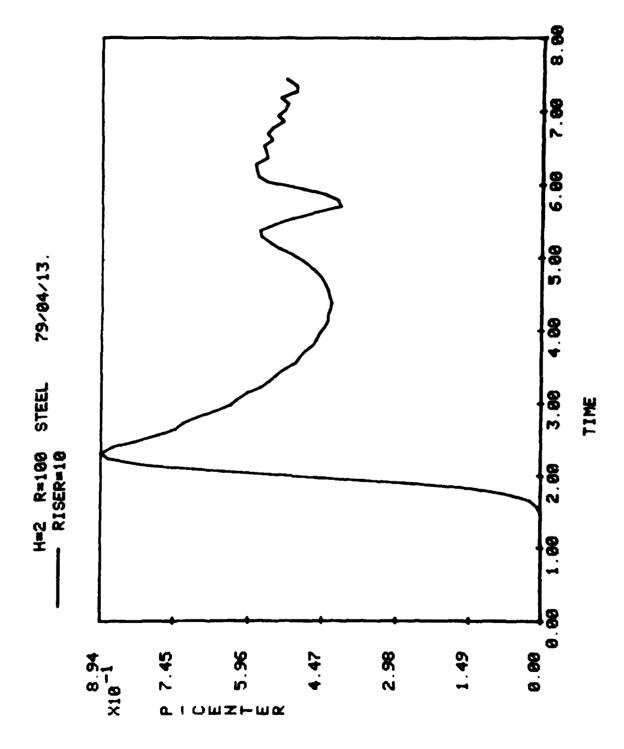
RING: Steel

Radius = 100 inches Thickness = 2 inches

Curve Label:	Meaning
P-CENTER:	pressure at $r = 0$
P-RIGHT:	pressure at $r = a/2$, $\theta = 0$
P-TOP:	pressure at $r = a/2$, $\theta = 90$ deg.
P-LEFT:	pressure at $r = a/2$, $\theta = 180$ deg.
SRV-RIGHT:	shell radial velocity at $\theta = 0$
SM-RIGHT:	shell moment at $\theta = 0$
SN-RIGHT:	shell stress resultant at $\theta = 0$
SRV-TOP:	shell radial velocity at θ = 90 deg.
STV-TOP:	shell tangential velocity at $\theta = 90$
SM-TOP:	shell moment at $\theta = 90$
SN-TOP:	shell stress resultant at θ = 90
SRV-LEFT:	shell radial velocity at θ = 180 deg.



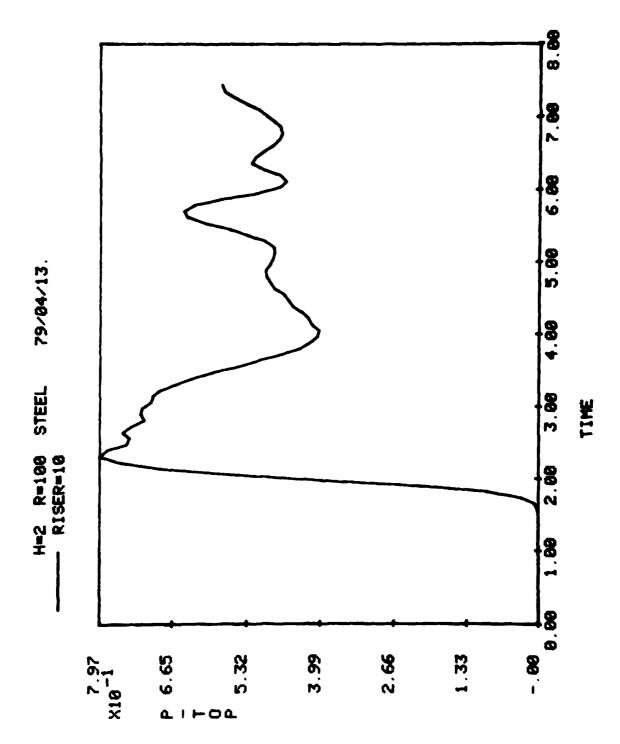
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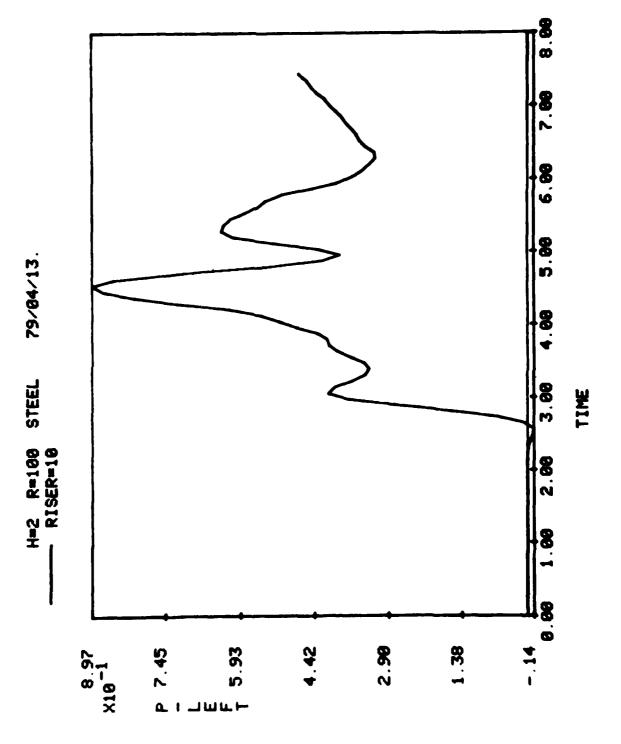


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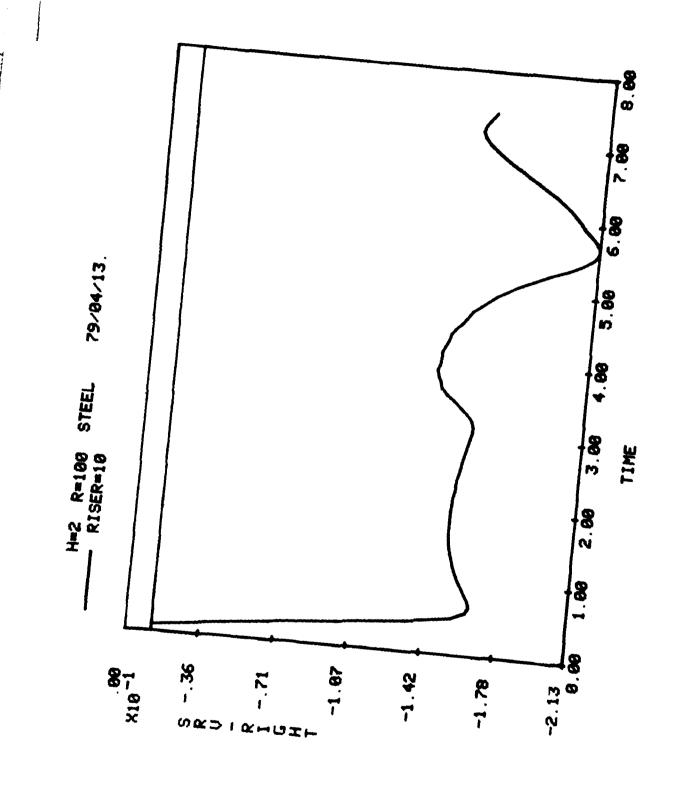
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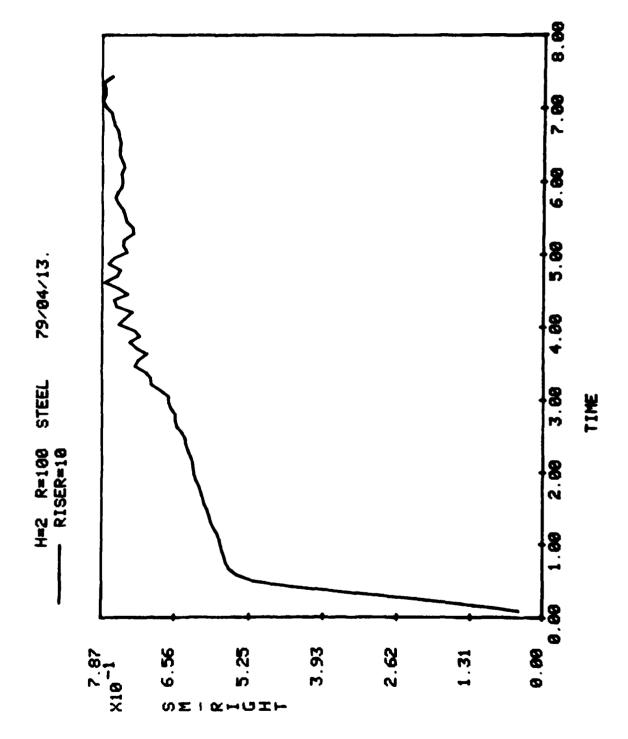
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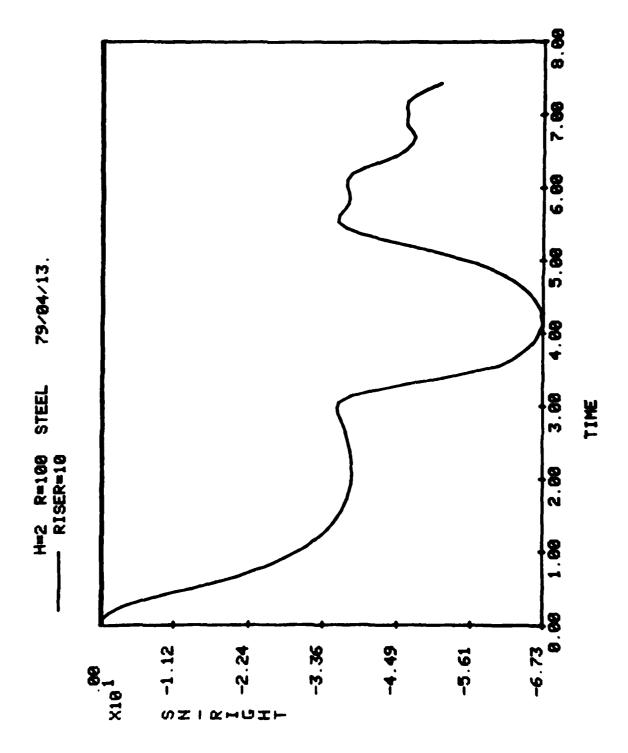


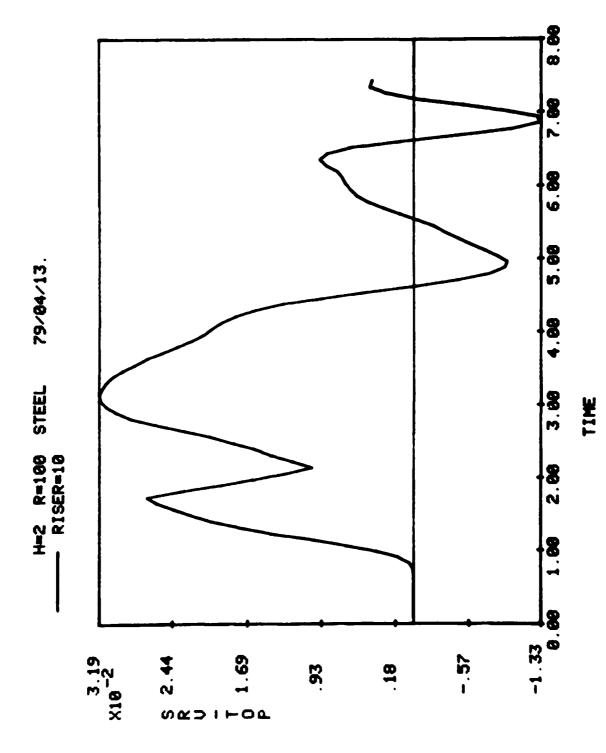


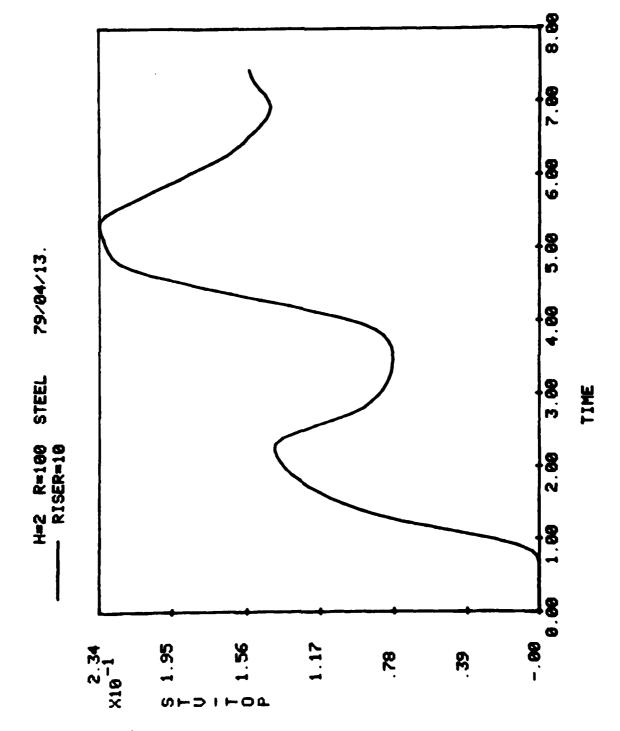
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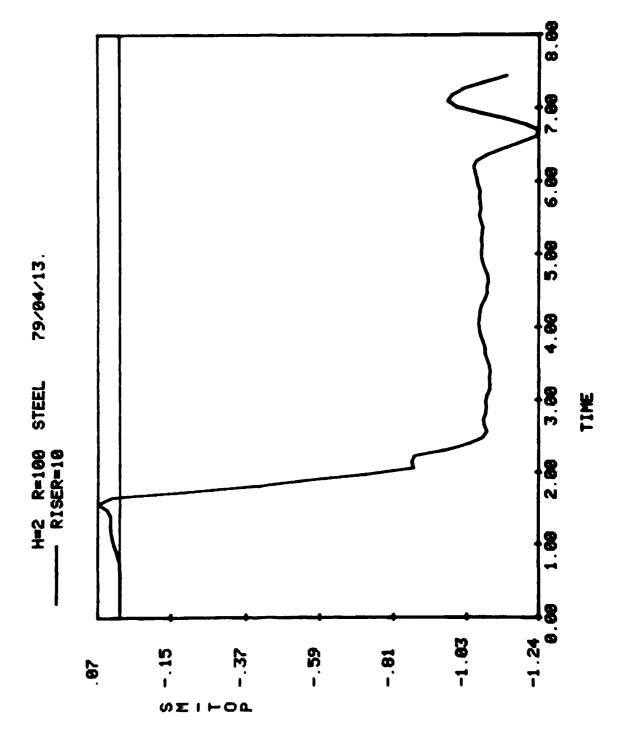




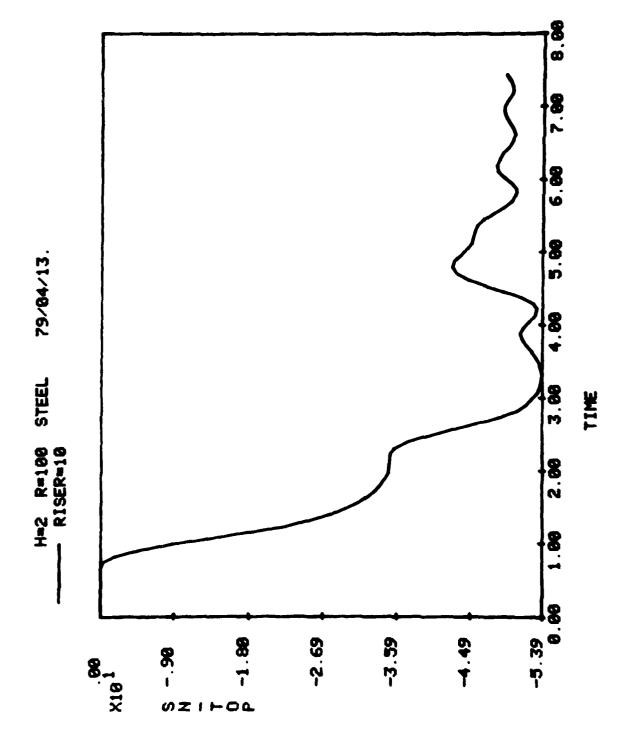








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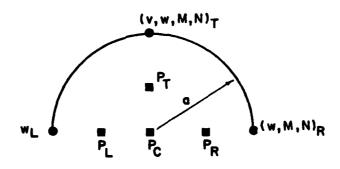
APPENDIX C (Case C)

RING: Steel

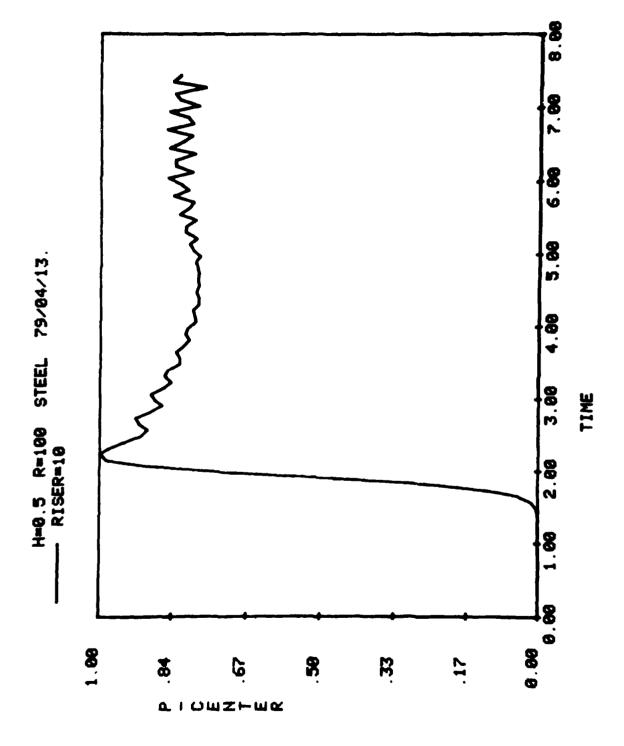
Radius = 100 inches Thickness = 0.5 inches

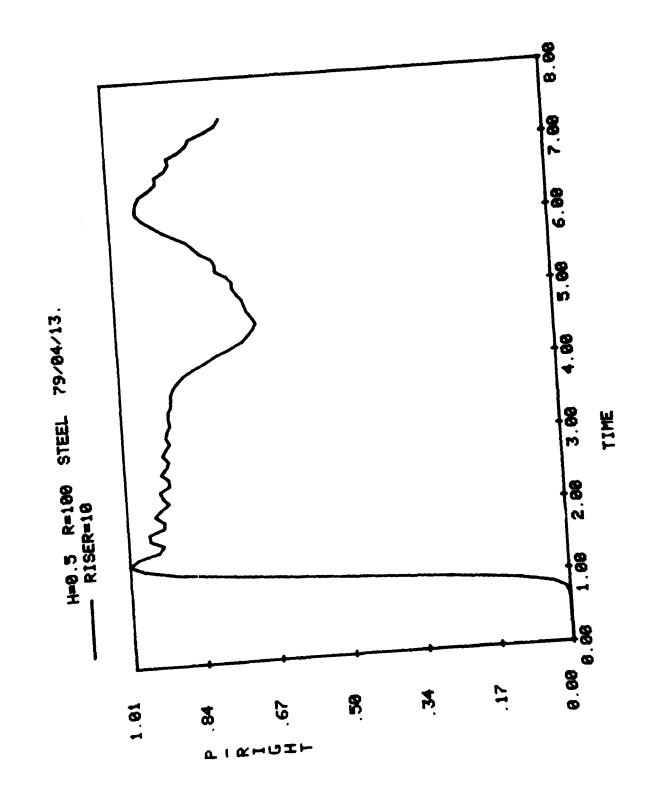
Curve Label: Meaning

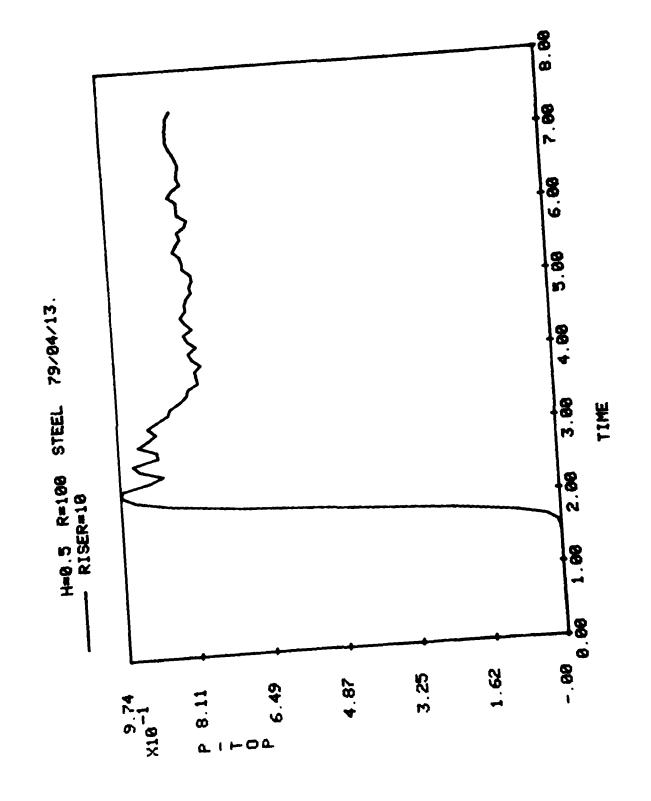
P-CENTER: pressure at r = 0pressure at r = a/2, $\theta = 0$ P-RIGHT: pressure at r = a/2, θ = 90 deg. P-TOP: P-LEFT: pressure at r = a/2, $\theta = 180$ deg. SRV-RIGHT: shell radial velocity at $\theta = 0$ shell moment at $\theta = 0$ SM-RIGHT: SN-RIGHT: shell stress resultant at $\theta = 0$ shell radial velocity at θ = 90 deg. SRV-TOP: STV-TOP: shell tangential velocity at $\theta = 90$ shell moment at θ = 90 SM-TOP: shell stress resultant at θ = 90 SN-TOP: SRV-LEFT: shell radial velocity at θ = 180 deg.

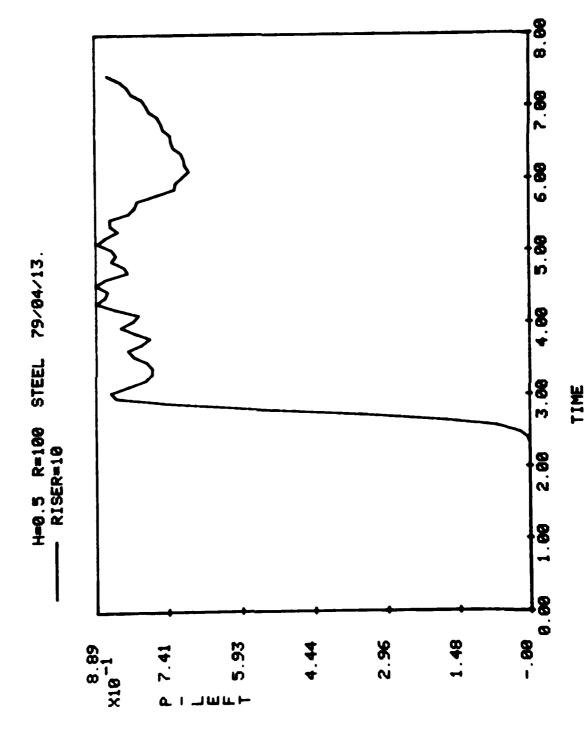


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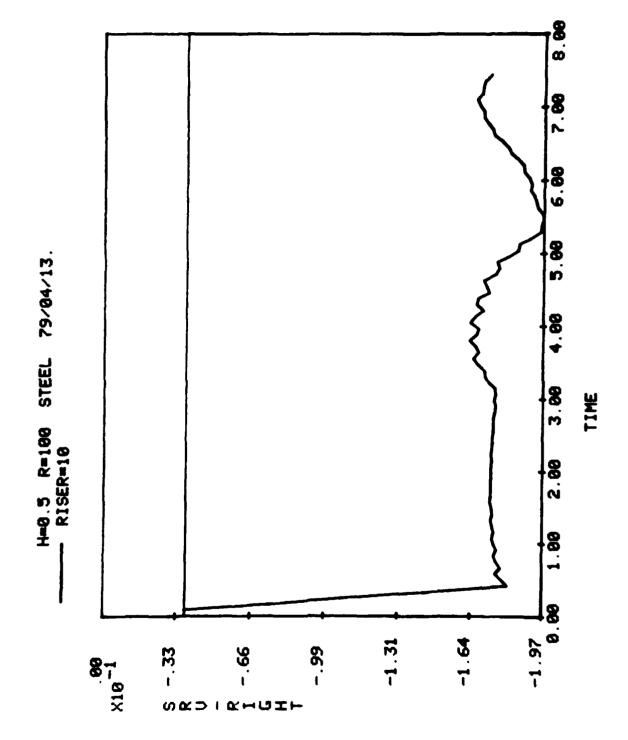




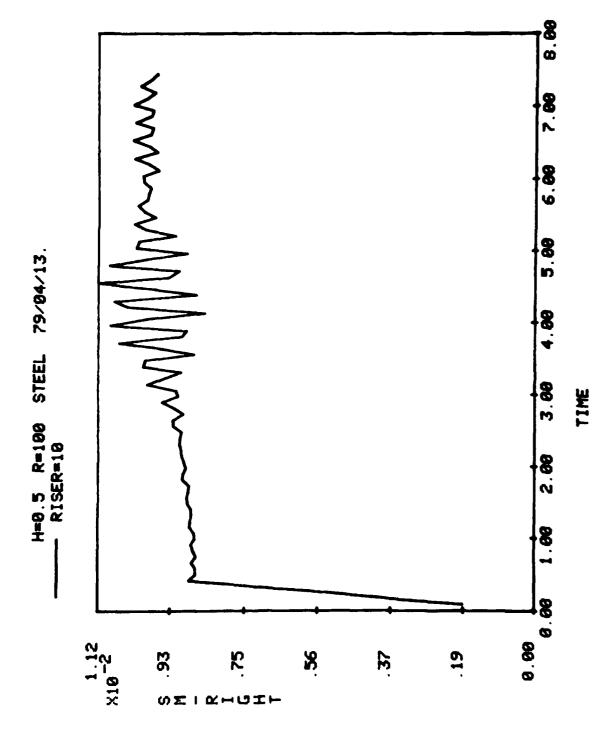




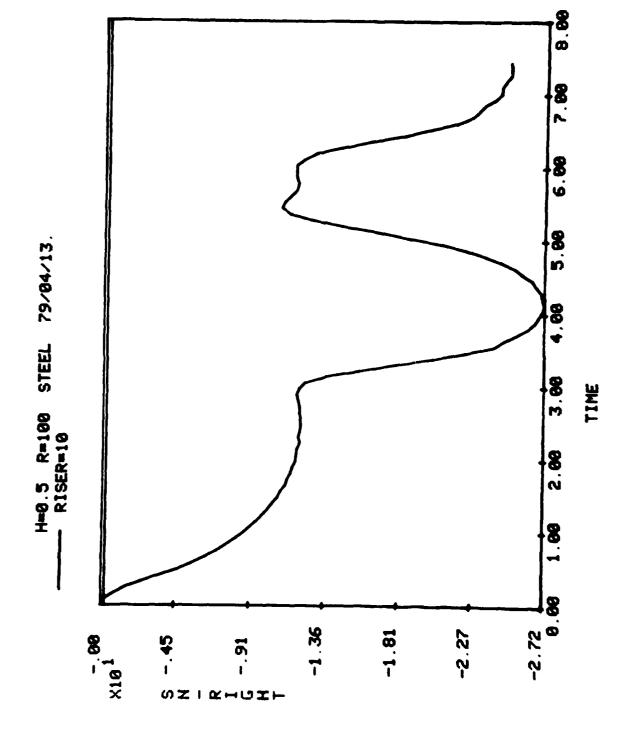
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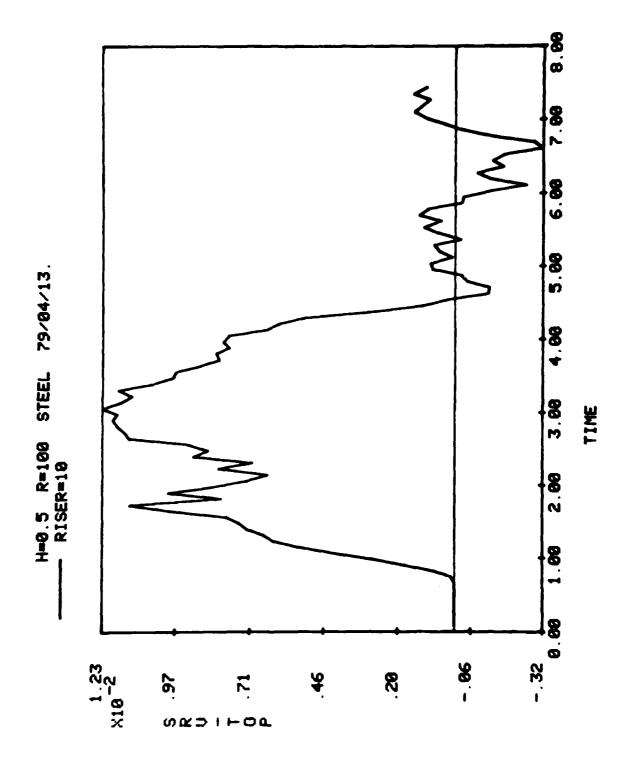


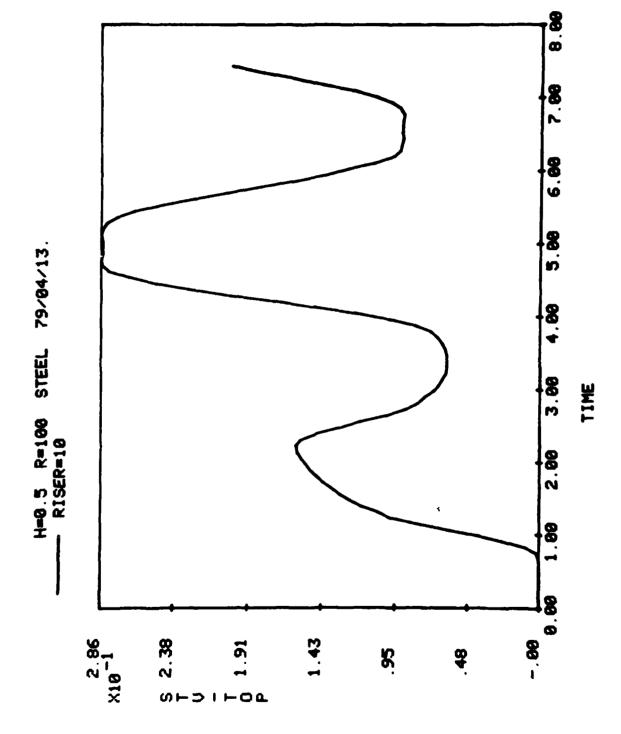
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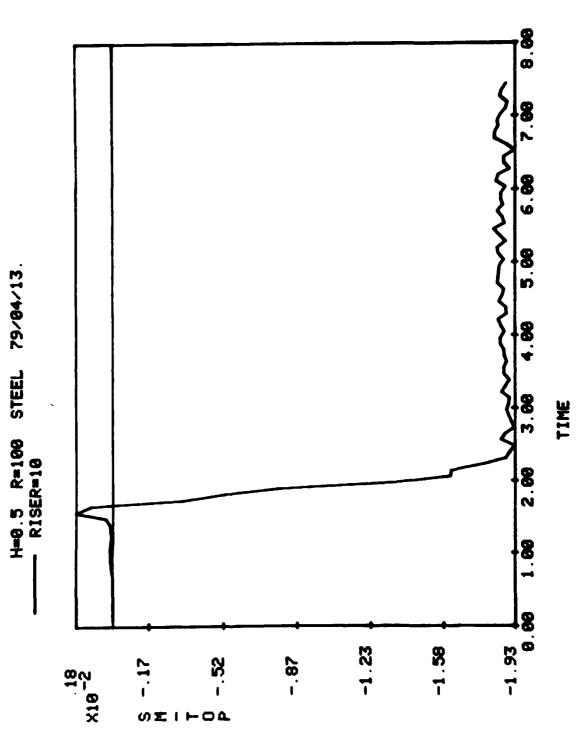
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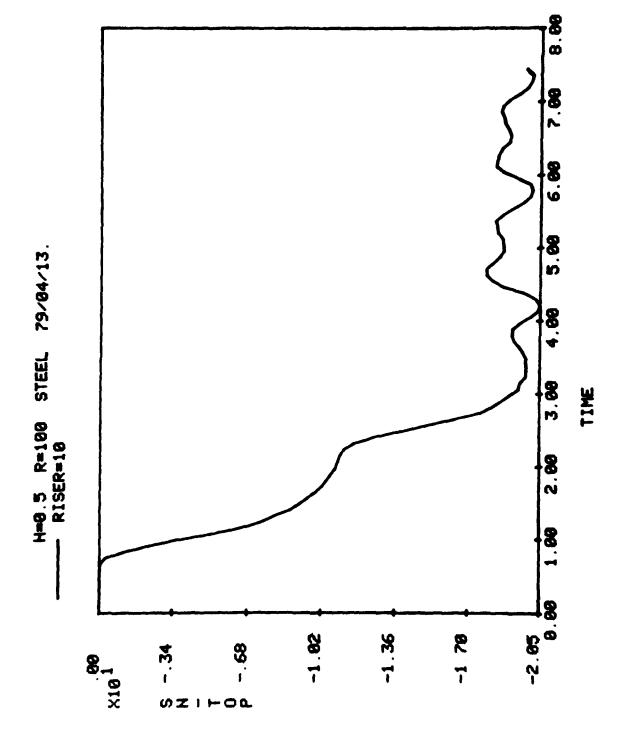


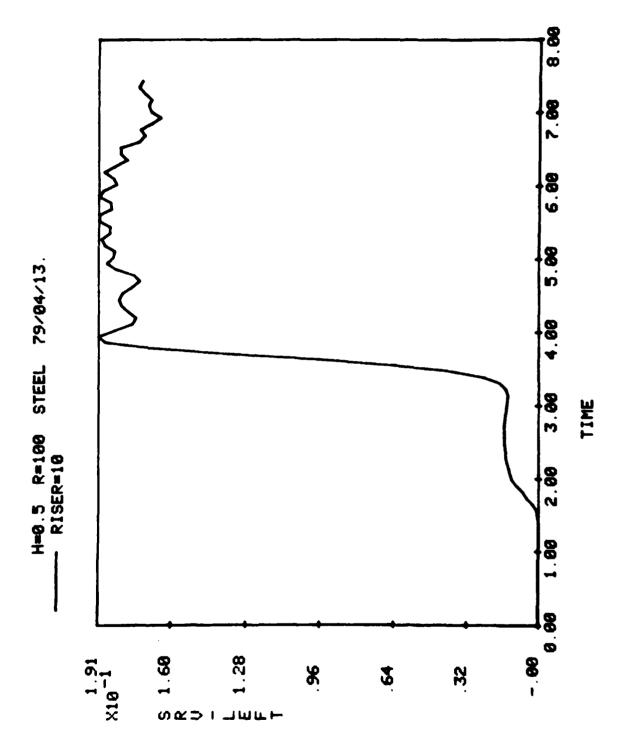










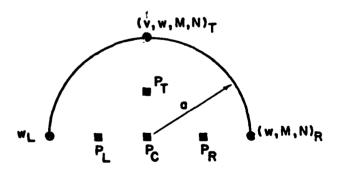


APPENDIX D (Case D)

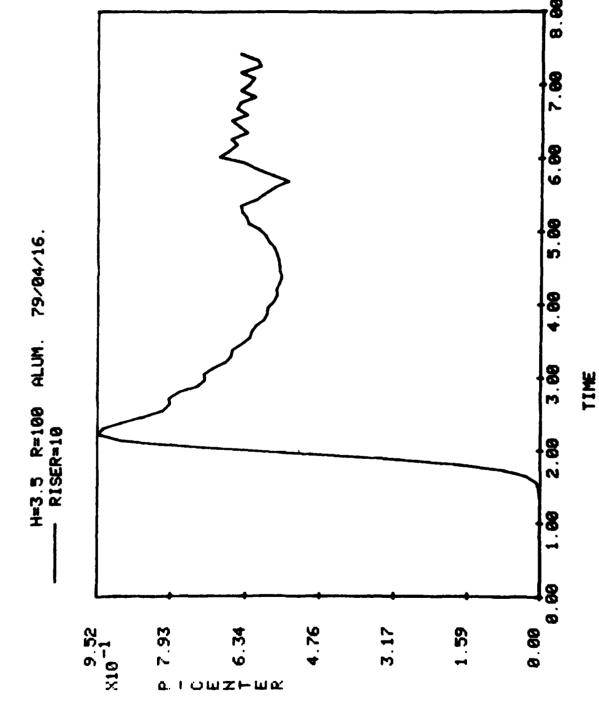
RING: Aluminum

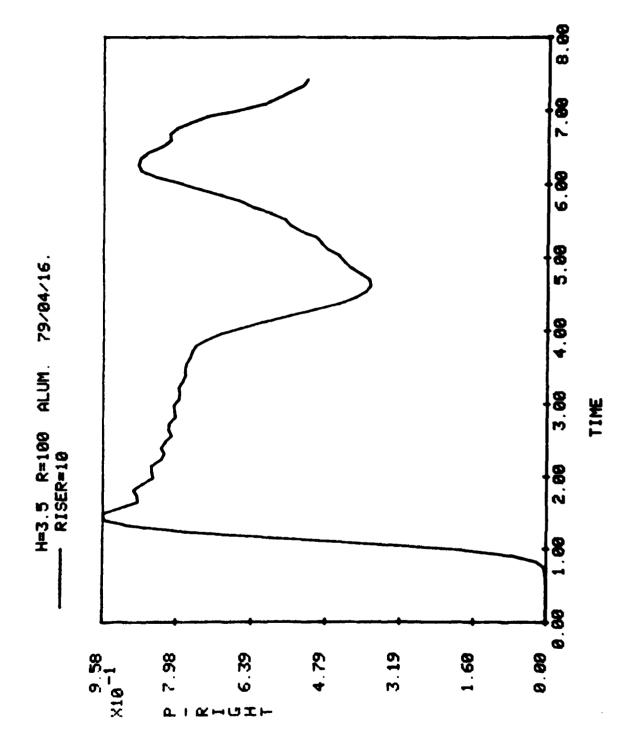
Radius = 100 inches Thickness = 3.5 inches

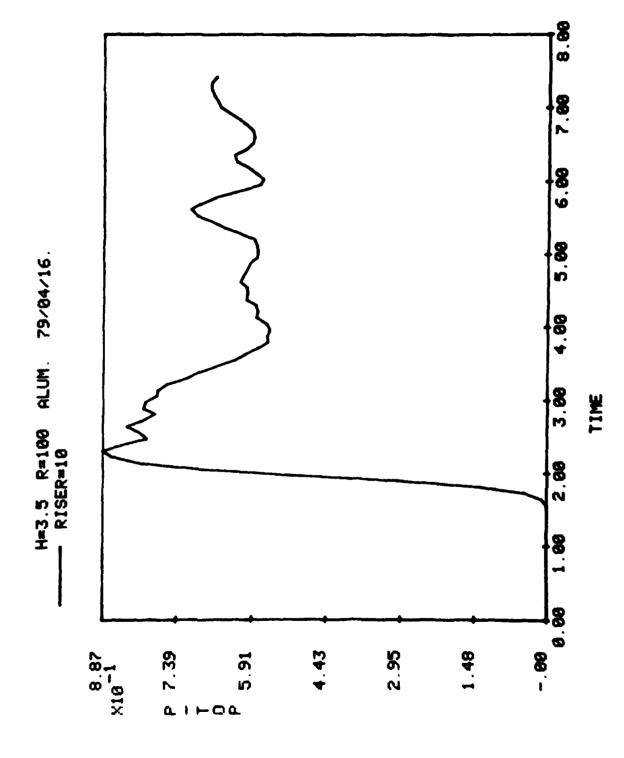
Curve Label:	Meaning
P-CENTER:	pressure at $r = 0$
P-RIGHT:	pressure at $r = a/2$, $\theta = 0$
P-TOP:	pressure at $r = a/2$, $\theta = 90$ deg.
P-LEFT:	pressure at $r = a/2$, $\theta = 180$ deg.
SRV-RIGHT:	shell radial velocity at $\theta = 0$
SM-RIGHT:	shell moment at $\theta = 0$
SN-RIGHT:	shell stress resultant at $\theta = 0$
SRV-TOP:	shell radial velocity at θ = 90 deg.
STV-TOP:	shell tangential velocity at $\theta = 90$
SM-TOP:	shell moment at θ = 90
SN-TOP:	shell stress resultant at $\theta = 90$
SRV-LEFT:	shell radial velocity at $\theta = 180$ deg.

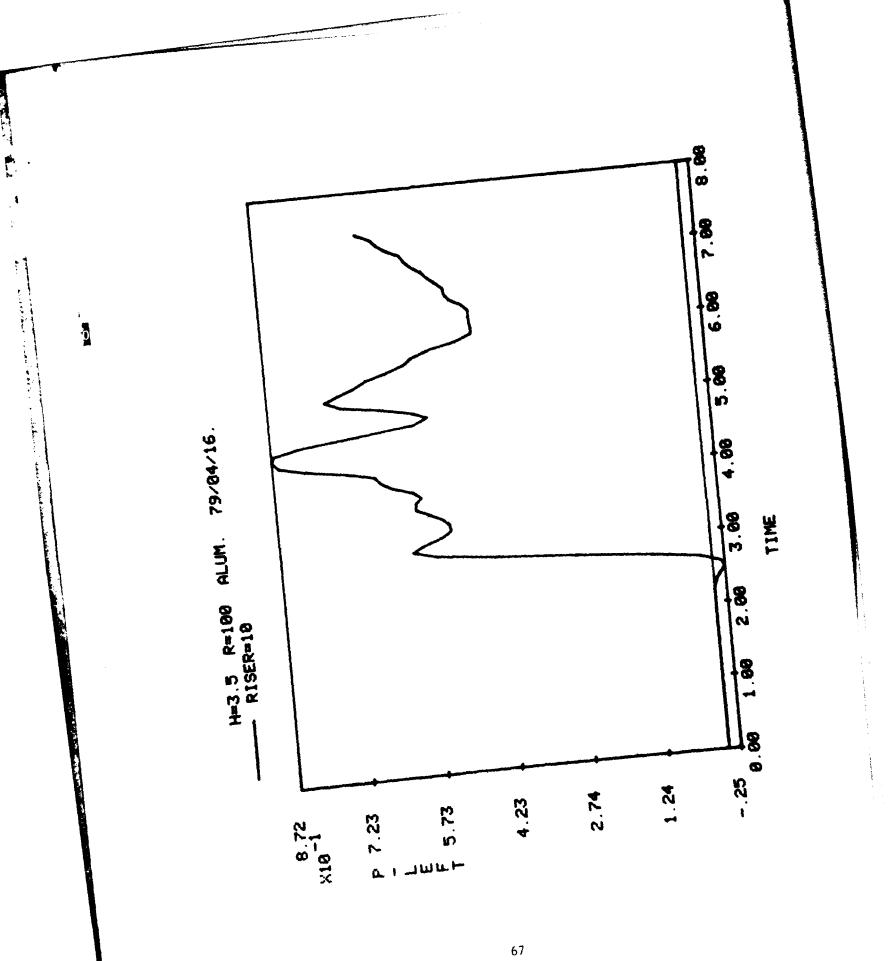


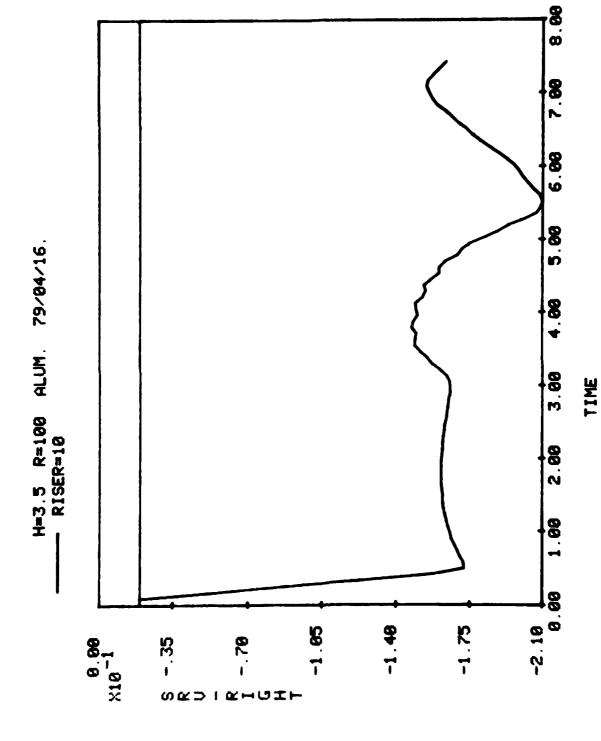
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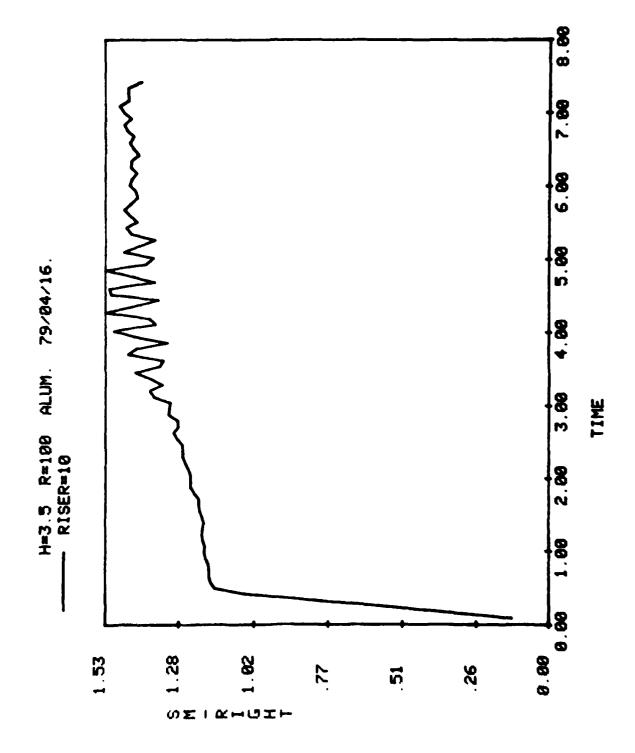


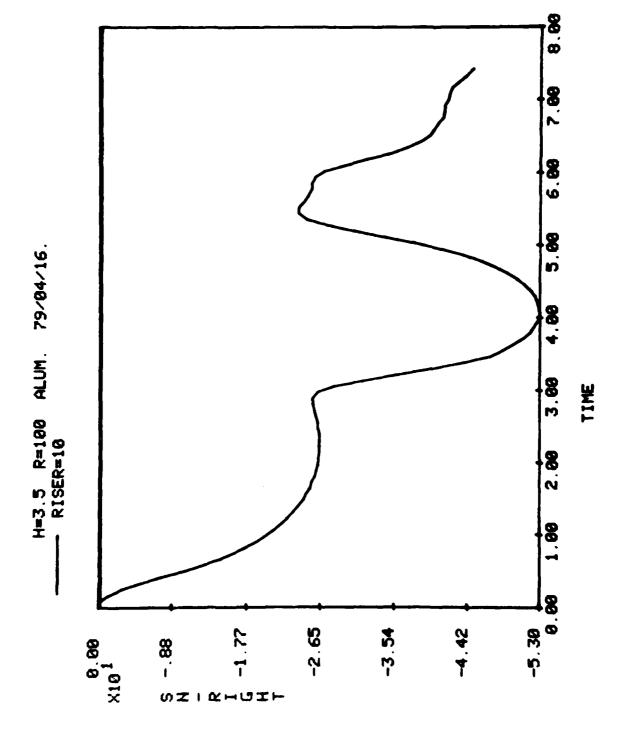




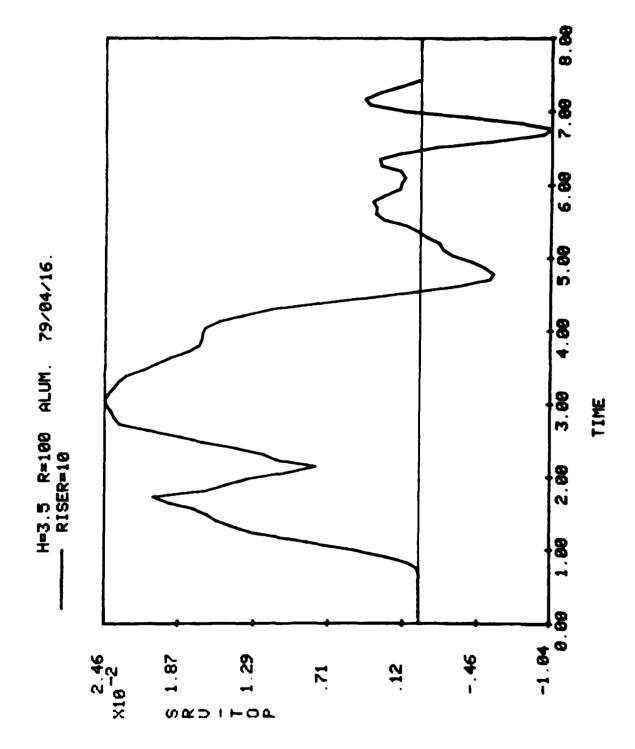


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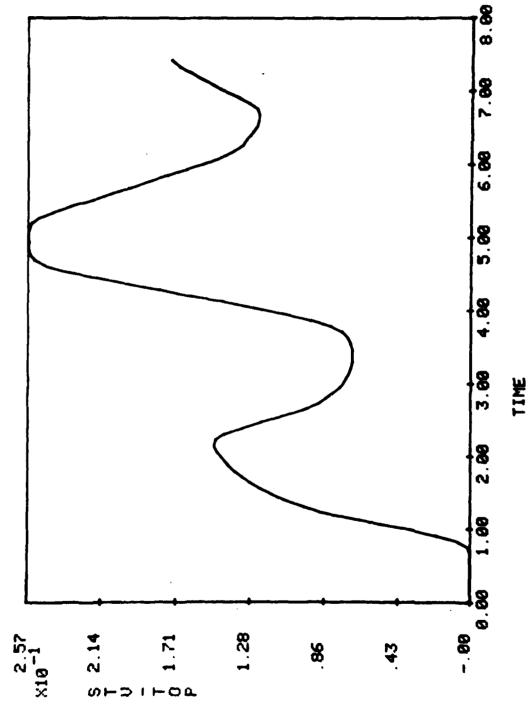


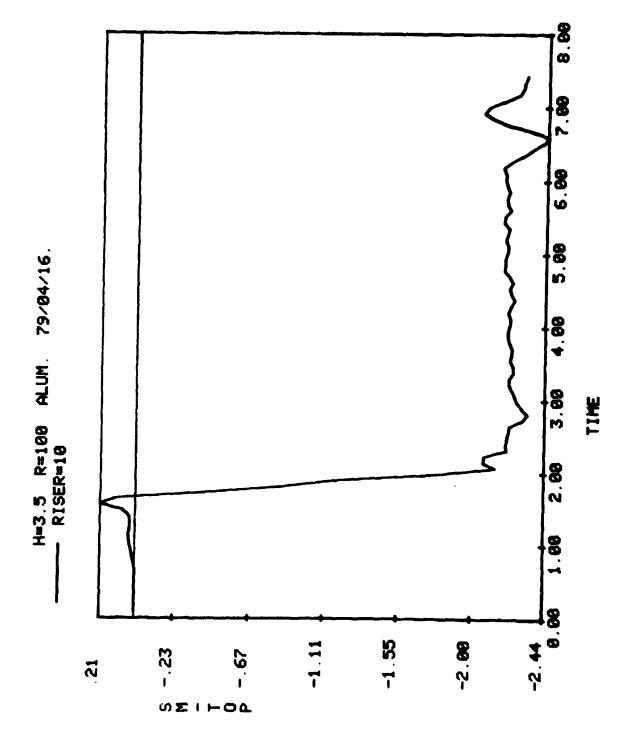


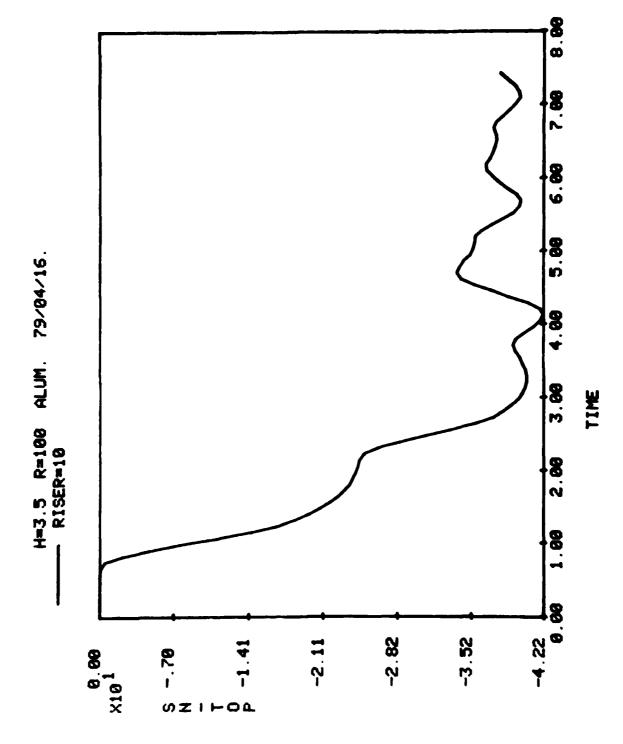
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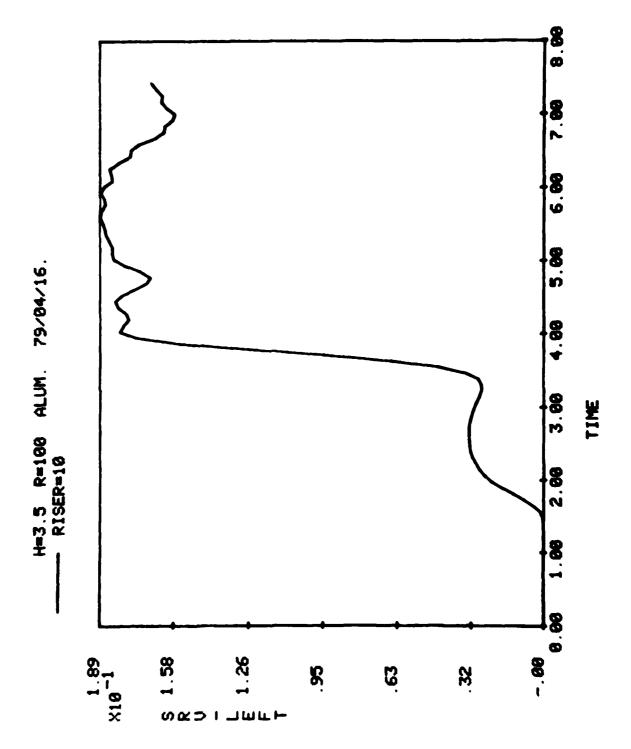








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APPENDIX E (Case E)

RING: Aluminum

Curve Label:

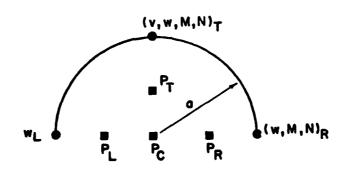
STV-TOP:

Radius = 100 inches Thickness = 1 inch

P-CENTER:	pressure at $r = 0$
P-RIGHT:	pressure at $r = a/2$, $\theta = 0$
P-TOP:	pressure at r = $a/2$, θ = 90 deg.
P-LEFT:	pressure at $r = a/2$, $\theta = 180$ deg.
SRV-RIGHT:	shell radial velocity at $\theta = 0$
SM-RIGHT:	shell moment at $\theta = 0$
SN-RIGHT:	shell stress resultant at $\theta = 0$
SRV-TOP:	shell radial velocity at θ = 90 deg.

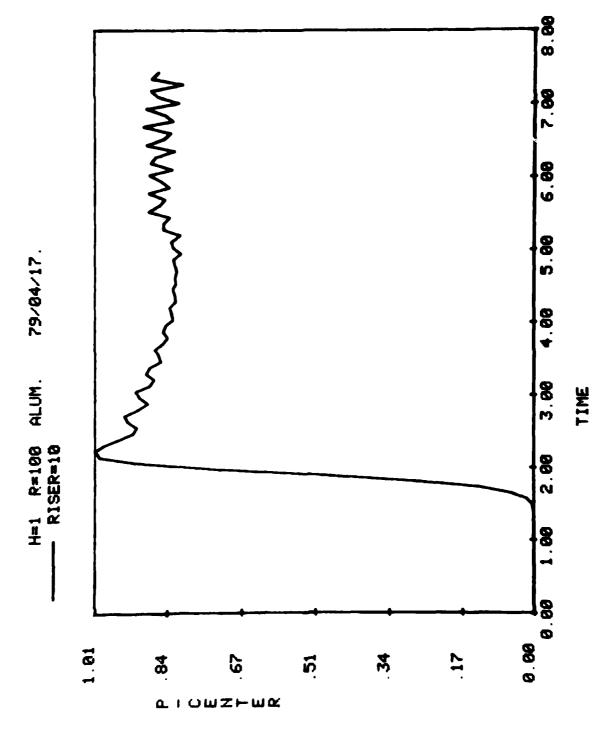
Meaning

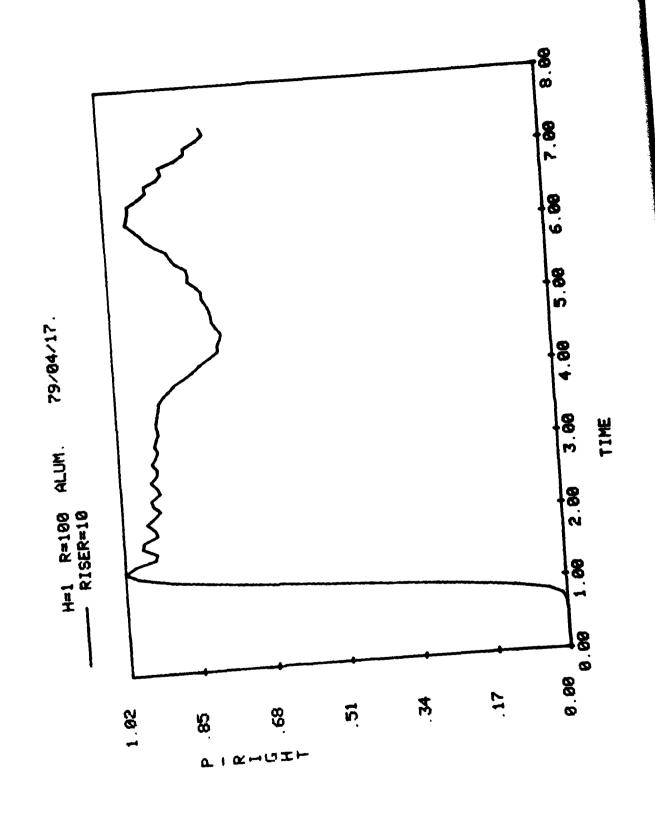
SM-TOP: shell moment at θ = 90 SN-TOP: shell stress resultant at θ = 90 SRV-LEFT: shell radial velocity at θ = 180 deg.

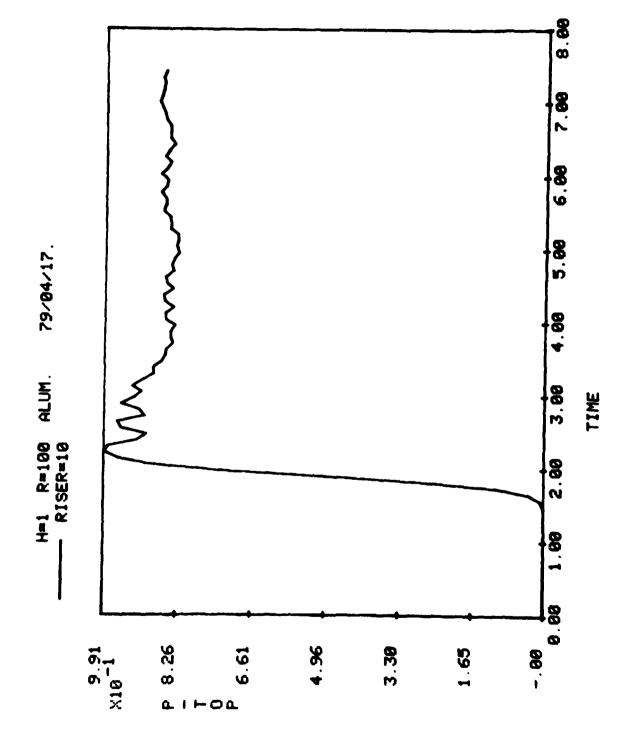


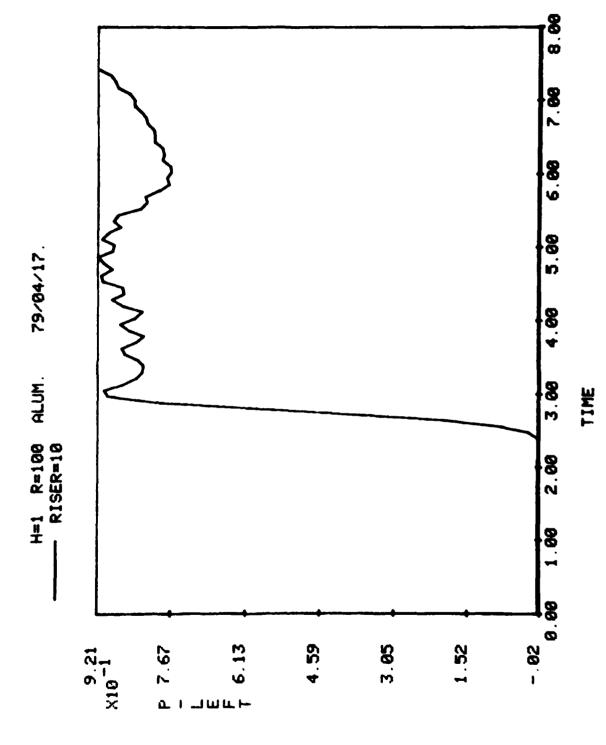
shell tangential velocity at $\theta = 90$

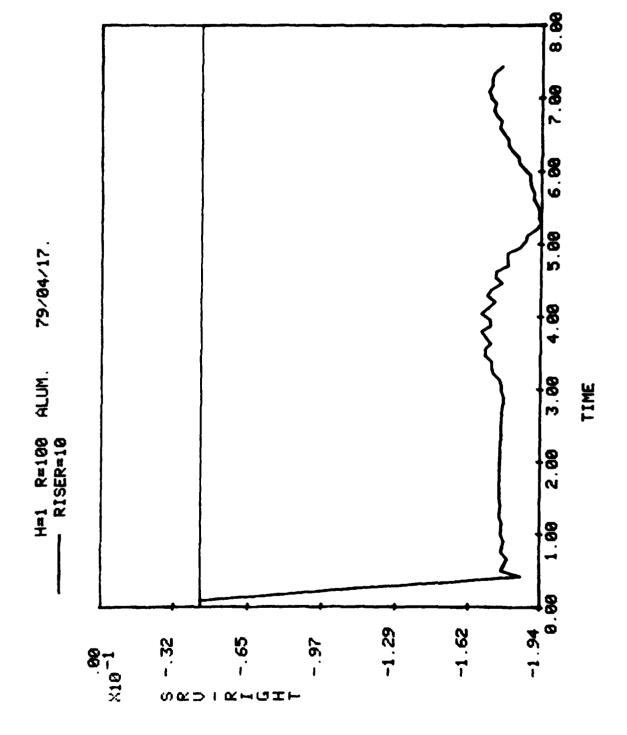
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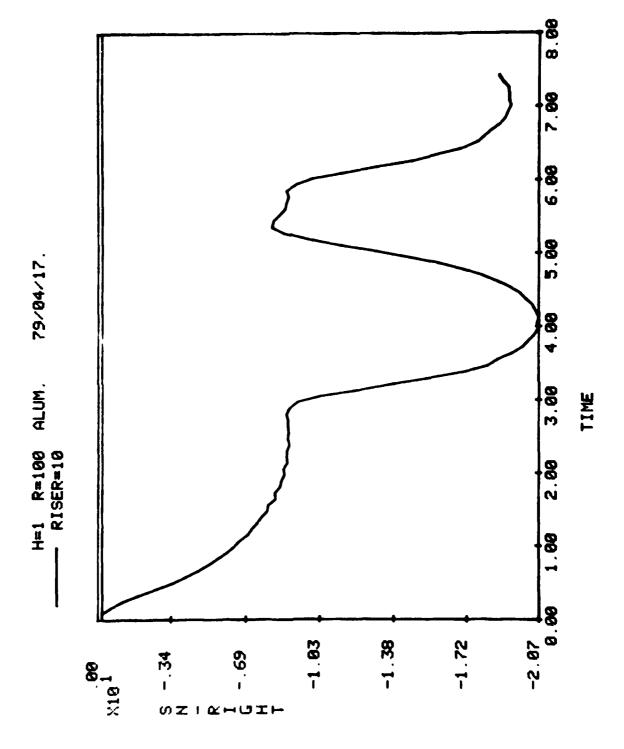


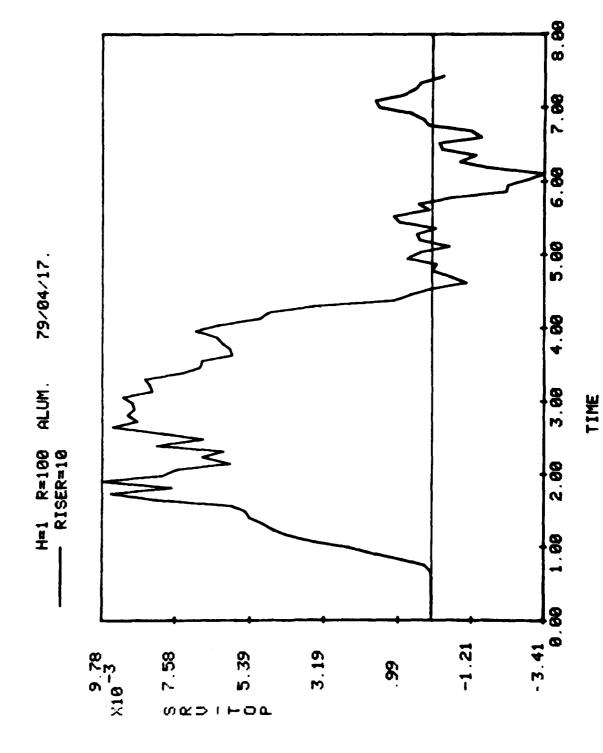


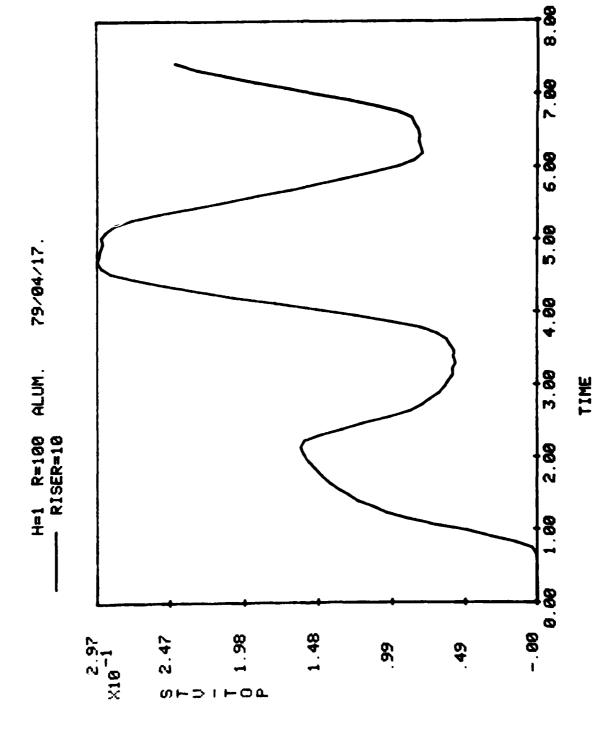


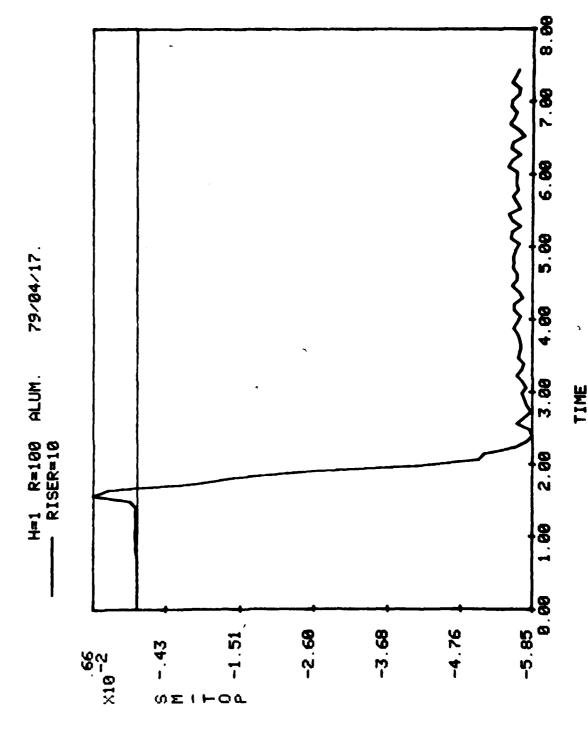


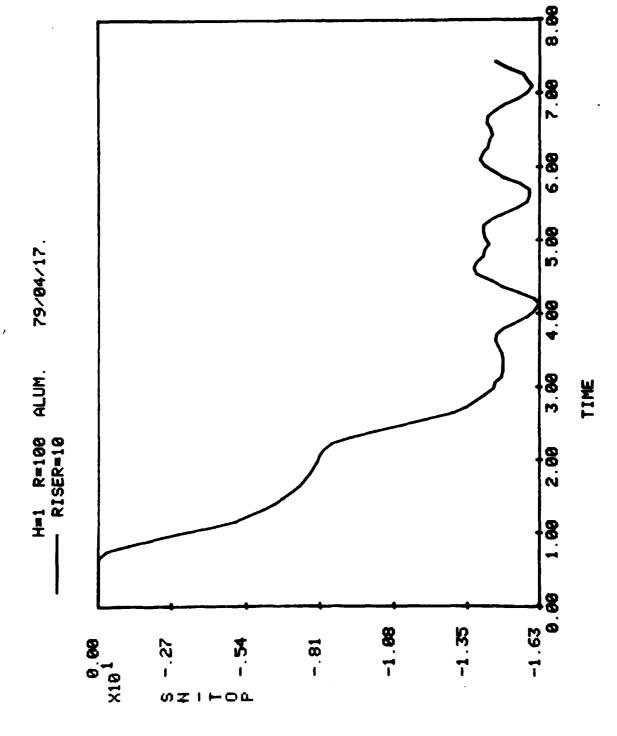




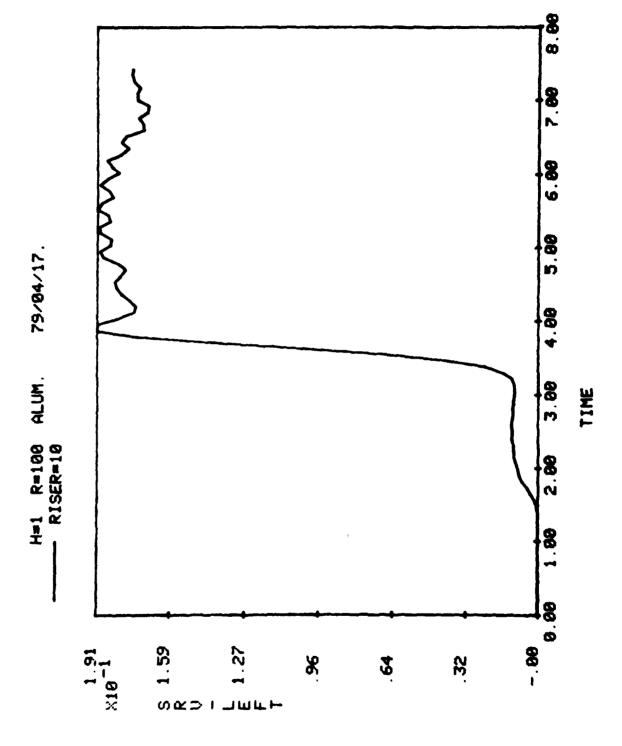








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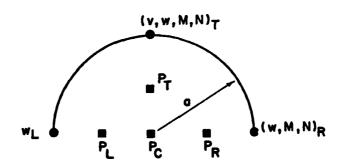


APPENDIX F (Case F)

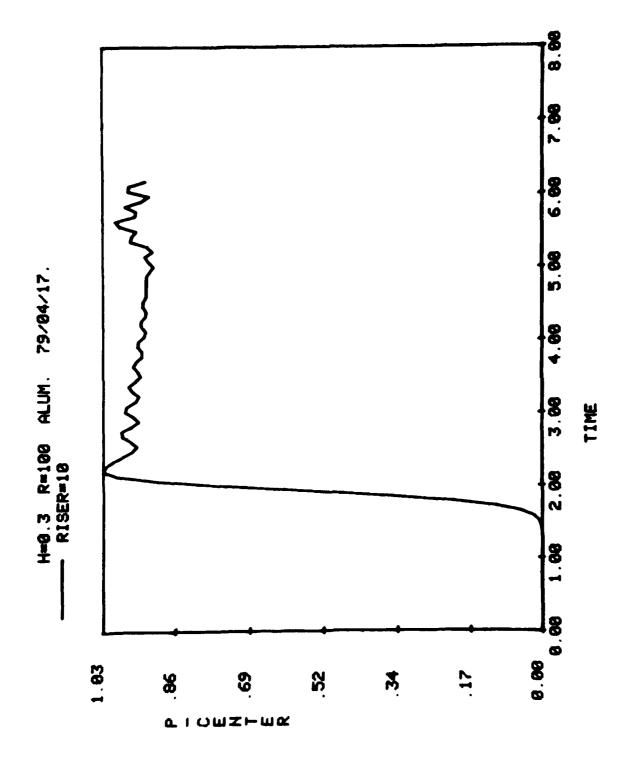
RING: Aluminum

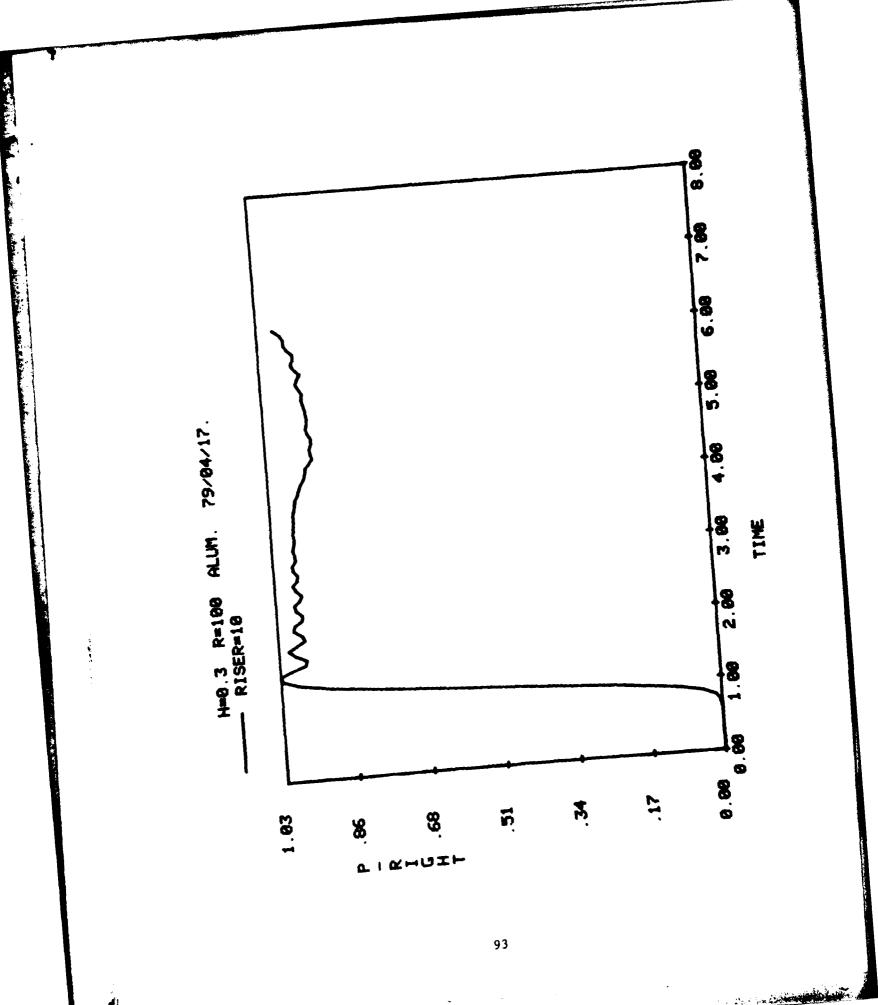
Radius = 100 inches Thickness = 0.3 inches

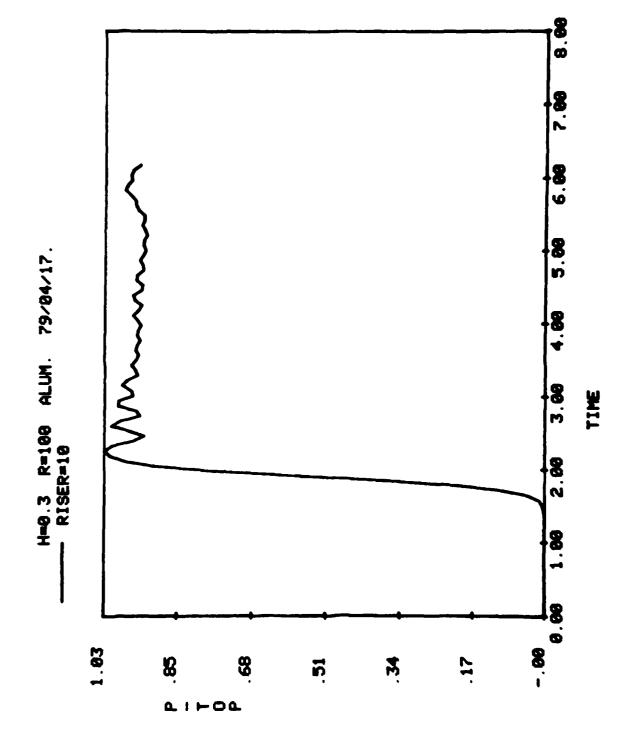
Curve Label:	Meaning
P-CENTER:	pressure at $r = 0$
P-RIGHT:	pressure at $r = a/2$, $\theta = 0$
P-TOP:	pressure at $r = a/2$, $\theta = 90$ deg.
P-LEFT:	pressure at r = $a/2$, θ = 180 deg.
SRV-RIGHT:	shell radial velocity at $\theta = 0$
SM-RIGHT:	shell moment at $\theta = 0$
SN-RIGHT:	shell stress resultant at $\theta = 0$
SRV-TOP:	shell radial velocity at θ = 90 deg.
STV-TOP:	shell tangential velocity at $\theta = 90$
SM-TOP:	shell moment at $\theta = 90$
SN-TOP:	shell stress resultant at $\theta = 90$
SRV-LEFT:	shell radial velocity at θ = 180 deg.



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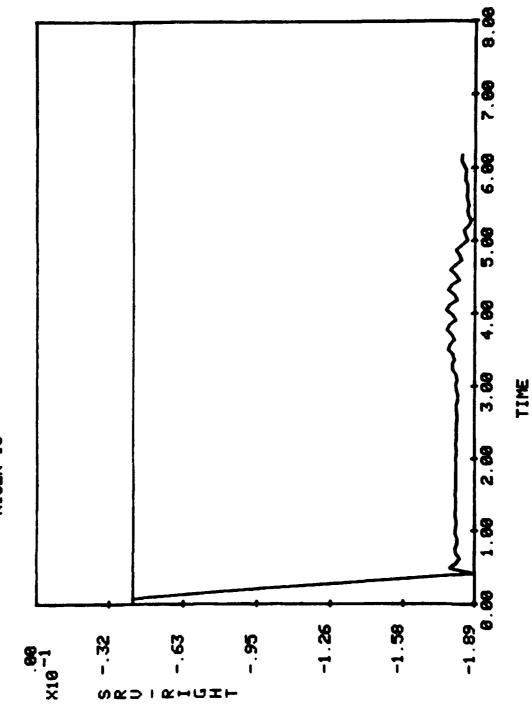


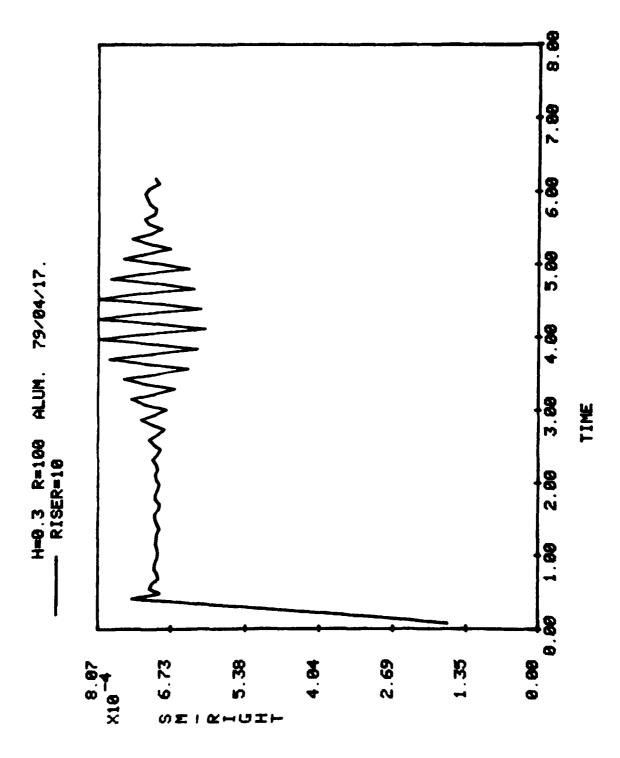




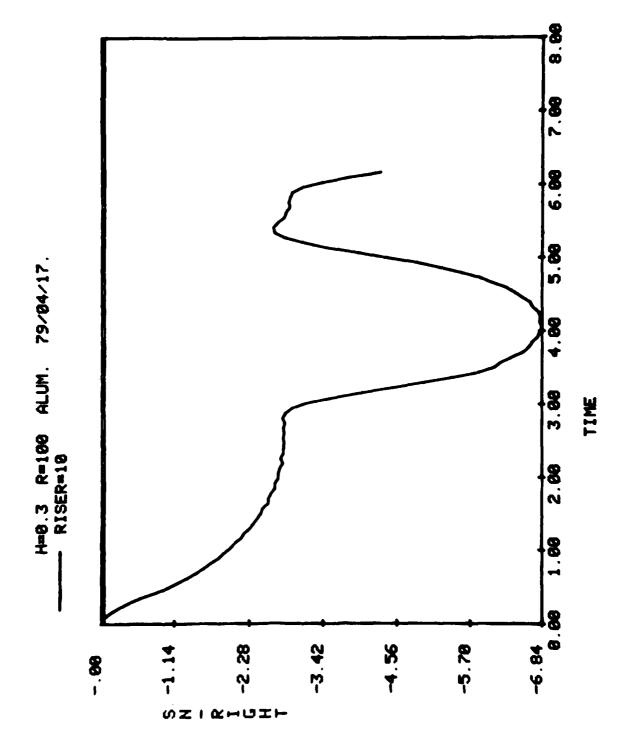
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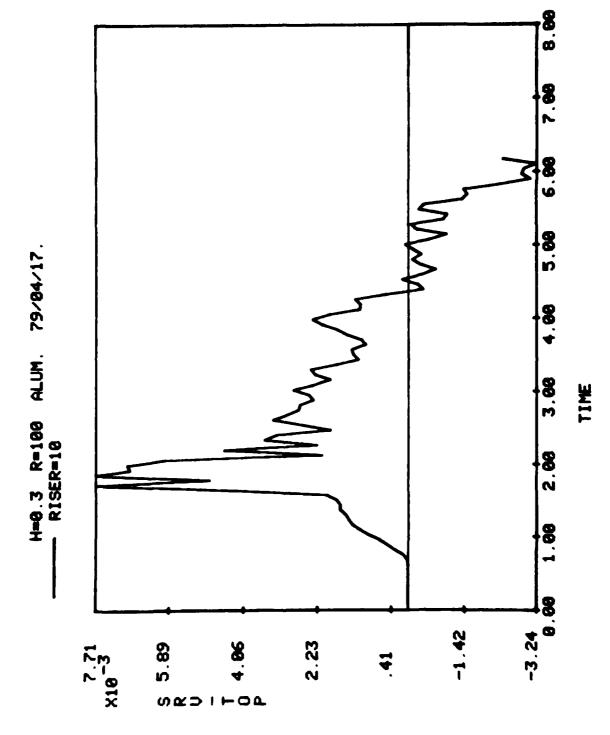


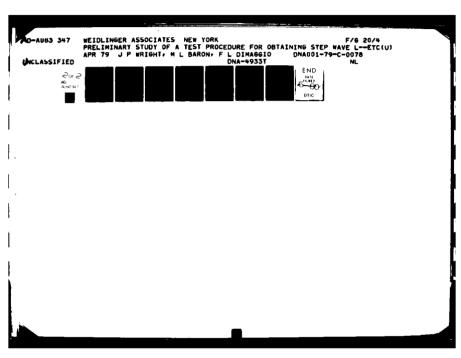


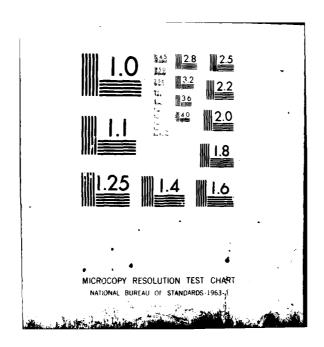


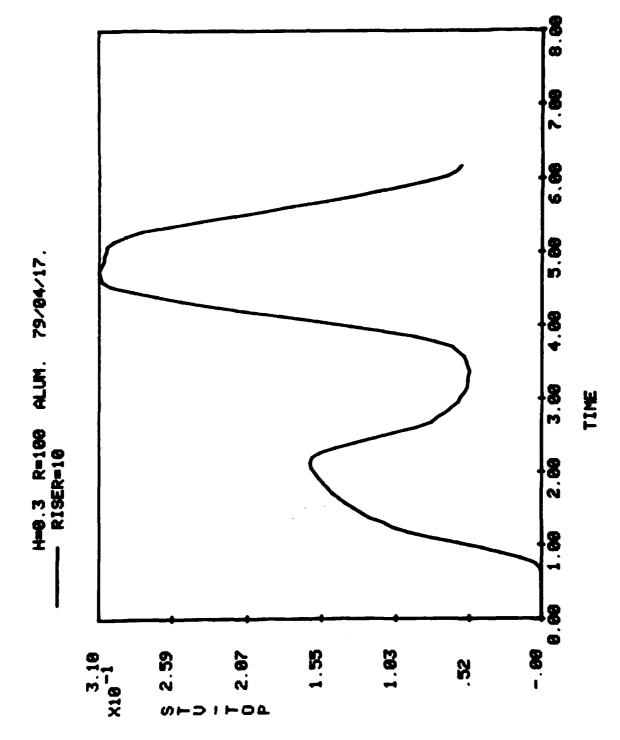
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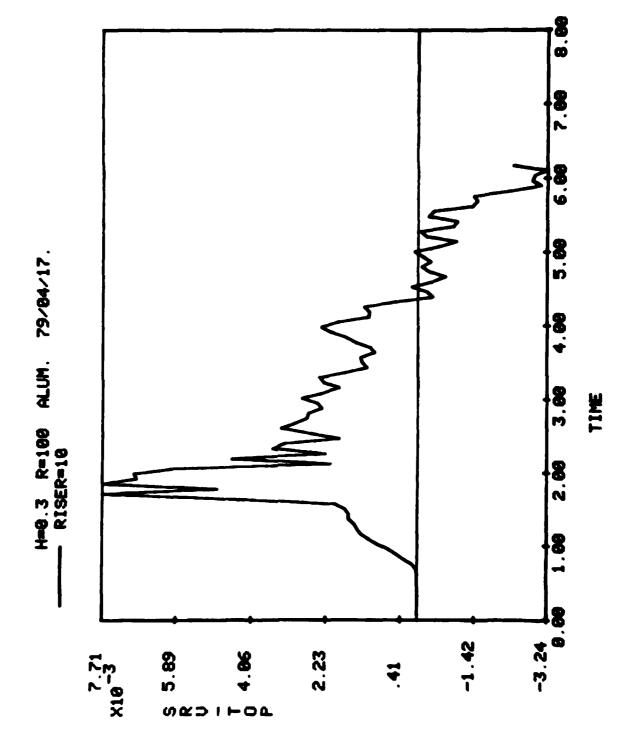


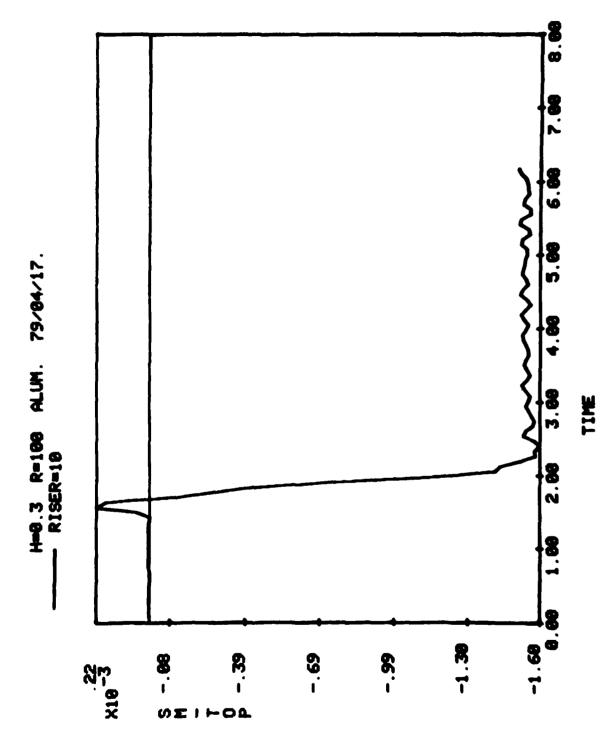


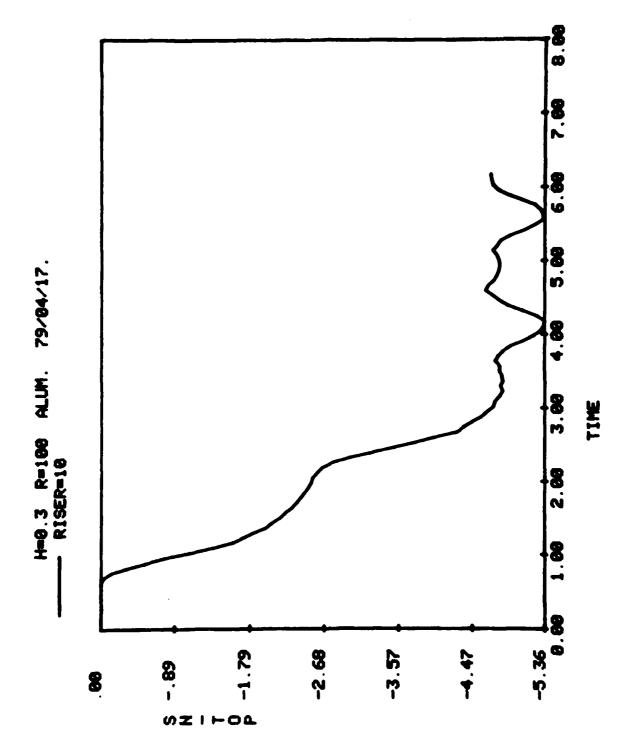


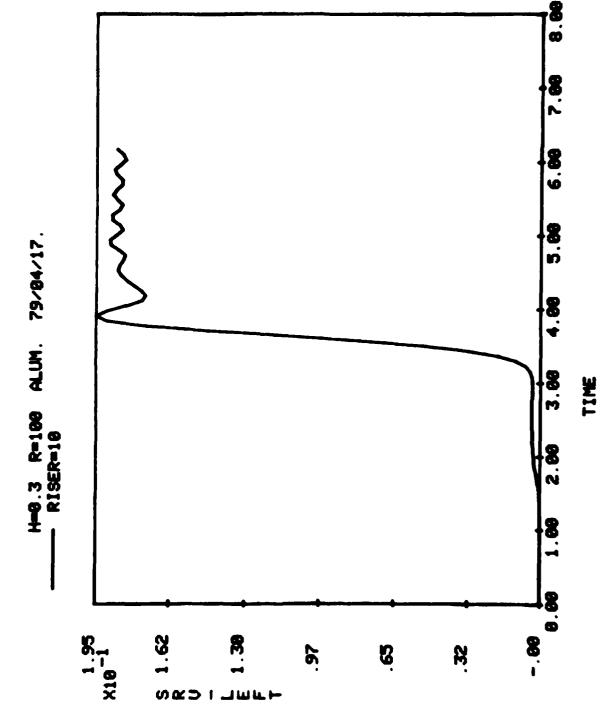












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